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ABSTRACT

This monograph covers the theory, application, and interpretation of both descriptive and inferential statistical techniques in institutional research. Each chapter opens with a hypothetical case study, which is used to illustrate the application of one or more statistical procedures to typical research questions. Chapter 2 covers the comparison of group means, including t-tests, one-way analysis of variance, factorial analysis of variance, analysis of covariance, multivariate analysis of variance, and nonparametric tests of mean differences. Chapter 3 covers correlation, and includes Pearson correlation coefficient, nonparametric correlations, and regression analysis. Chapter 4 covers chi-square: two-way chi square, one-way chi square, and chi-square automatic interaction detection. Chapter 5, which covers selection of the appropriate statistic, discusses and gives examples of design trees. The appendix lists the statistical commands in the Statistical Package for the Social Sciences that are used to perform the analyses illustrated in the text. (Contains 15 references.) (CH)

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CASE STUDY APPLICATIONS OF STATISTICS IN INSTITUTIONAL RESEARCH

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By MARY ANN COUGHLIN and MARIAN PAGANO

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Case Study Applications of Statistics in Institutional Research

by
Mary Ann Coughlin
and
Marian Pagano

Number Ten
Resources in Institutional Research

A JOINT PUBLICATION OF
THE ASSOCIATION FOR INSTITUTIONAL RESEARCH
AND
THE NORTHEAST ASSOCIATION FOR INSTITUTIONAL REASEARCH

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Case Study Applications of Statistics in Institutional Research

Introduction

Statistics has been defined as "a collection of methods for planning experiments, obtaining data, and then organizing, summarizing, presenting, analyzing, interpreting and drawing conclusions based on the data" (Triola, 1995, p. 4). Does this sound like an abbreviated charge for the Office of Institutional Research at your institution? Saupe (1990) discussed several of the above-mentioned activities as functions of Institutional Research. He encapsulated this view by defining Institutional Research as "research conducted within an institution of higher education to provide information which supports institutional planning, policy formation and decision making" (p. 1).

While statisticians are more likely to disagree than agree on a variety of issues, general agreement exists that the field consists of two subdivisions: descriptive and inferential statistics. Descriptive statistics consists of a set of techniques for the important task of *describing* characteristics of data sets and for summarizing large amounts of data in an abbreviated fashion. Inferential statistics goes beyond mere description to draw conclusions and make inferences about a population based on sample data. While most Institutional Researchers are quite knowledgeable in the area of descriptive statistics, many are less comfortable with inferential techniques. The use of inferential techniques can bring critical enlightenment to policy and planning decisions.

Thus, this monograph focuses on the application of statistical techniques to Institutional Research; theory, application, and interpretation are the main tenets. The ultimate goal of the authors is to enhance the researchers' knowledge and interpretation of their data through statistical analyses. The text begins with a general background discussion of the nature and purpose of both descriptive and inferential statistics and their applications within Institutional Research. Each additional chapter follows a case study format and outlines a practical research question in Institutional Research, illustrates the application of one or more statistical procedures, analyzes data representing a hypothetical institution, and incorporates the output from these analyses into information that can be used in support of policy- and decision-making.

This document is designed to give the reader a broad overview of or refresher in descriptive and inferential statistics as they are applied to case studies in Institutional Research. In this format, this is quite a challenge as a wide range of statistical concepts and procedures is covered in relatively few pages. No intent is made to document the numerical calculation of statistics or to prove statistical formulas. For further information in any of these areas, please consult the list of references.

Statistical software packages are standard equipment in most Institutional Research offices as they handle complex analyses and large data files relatively effortlessly. While it is important that an Institutional Researcher be able to use statistical packages, this monograph is not designed to teach you how to do so. Rather, the emphasis of this monograph will be on the theory, application, and interpretation of statistical analyses. Many statistical packages are available on a wide range of computer platforms that can be utilized to perform these analyses. The Statistical Package for the Social

Sciences (SPSS) is the choice of the authors for statistical software and SPSS for Windows was used to analyze the data from each case study, yet any standard statistical software can perform these analyses. For your convenience, the statistical commands that perform the analyses discussed in this text using SPSS for Windows are included in Appendix A. These commands can be readily translated into any standard statistical software.

Before proceeding to the main text, some practical limitations of this monograph should be declared. The first and most important of these points is that the best statistics cannot save an inferior research design. Statistical procedures are no substitute for forethought. Although several robust research designs are illustrated throughout this text, the primary emphasis of the monograph is not dedicated to design concepts. Suffice it to say that the research design is the foundation of a good study. If the design is weak, the analysis will crumble. Remember, the statistician's favorite colloquial expression: **"Garbage in, Garbage out."** Secondly, the topics and techniques covered in this text are for the most part standard and accepted practices. However, as in most fields, few absolutes exist with many differing opinions. Please feel free to review the references for other suggested practices and approaches to the tasks presented here.

Finally, the case studies and example data utilized in this text are fabricated studies representing fictitious institutions, but are designed to represent real research questions facing Institutional Researchers. In no way should the case studies or data be associated with the authors or the institution of the authors. In the real world, the questions facing individual Institutional Researchers are as varied as the researchers themselves and their respective institutions. Yet the case studies have been carefully developed to represent the diversity in our profession and to present a variety of statistical procedures with universal application.

Chapter One: Basic Concepts

This chapter is designed to give a brief overview of some basic statistical concepts and terms that will be used throughout this text and is divided into the following four sections: Characteristics of Variables and Levels of Measurement; Descriptive Statistics; Probability, Sampling Theory and the Normal Distribution; and Inferential Statistics. While the titles of these sections imply that this chapter will cover all the material taught in an Introductory Statistics text, please be advised that the text flows briskly through each of the topics and is meant to serve only as a refresher. For more detailed information, please refer to Sprinthall (1987), Levin and Fox (1994), Triola (1995) or any basic statistical textbook.

Characteristics of Variables & Levels of Measurement

A variable is an indicator or measure of the construct of interest. A variable can be anything that has more than one value (e.g., sex, age, SAT scores). Variables should have operational definitions clearly stated. An operational definition of a variable defines specifically the variable measured and, unless it is a universally accepted definition, should be clearly published with any data and analyses. For example, when using SAT scores from an inquiry survey, SAT score could be operationally defined as **"the self-reported scores on both the math and verbal sections of the SAT examination."** This alerts the reader that the results from this analysis might vary from results reported from the Educational Testing Service. For other examples, refer to Example Box 1.

Example Box 1

Variable	Operational Definition
FTE - Faculty	Total number of full time faculty plus ⅓part-time faculty headcount
Student	Anyone enrolled during a semester for at least 1 credit hour
Compensation	Salary plus fringe benefits

While this operational definition is quite straightforward, some operational definitions get sticky and lead to the issue of construct validity. Many constructs or concepts in educational research are wide-open to interpretation. Institutional Researchers are usually quite familiar with the nuances of construct validity as we deal with the definition of FTE, full-time faculty, and other seemingly simple variables whose definitions are often capricious. The important point is to clearly communicate how you have measured the constructs (i.e., the underlying variables) in your design.

The ***values*** contained within a variable are often determined by the researcher. This is a critical decision in the research design phase, and influences the possibilities for statistical analysis as these values define the level of measurement for that variable. A variable can have continuous or discrete values. Variables are discrete when they have a finite or countable number of possible values. For example, gender, ethnic background, and student status (i.e., full-time / part-time) are discrete. Continuous variables have infinite range and can be measured to varying degrees of precision. Common examples of

continuous data are dollars, square footage, height, weight, and age. A continuous variable may be measured as if it were discrete; however, the reverse is not true. For example, salary data can be broken down into discrete categories (Example Box 2). In some instances, dividing a discrete variable by a discrete variable creates a continuous scale; for example, admissions yield ratios (number enrolled divided by number applied).

Example Box 2

Salary as a Discrete Variable	Salary as a Continuous Variable
$1 - $25,000 $25,001 - $50,000 Over $50,00	Actual Salary in dollars $42,014

Levels of measurement can be further broken down into a hierarchy with four categories: nominal, ordinal, interval, and ratio. Variables which are *Nominal* level of measurement consist of names, labels and categories; this is the lowest level of the hierarchy. In classifying data, subjects or observations are identified according to a common characteristic. When dealing with a nominal variable, every case or subject must be placed into one and only one category. This requirement indicates that the categories must be non-overlapping or mutually exclusive. Thus, any respondent labeled as **male** cannot also be labeled as **female**. Also, this requirement indicates that categories must be exhaustive; that is, a place must exist for every case that arises. Nominal data are not graded, ranked or scaled in any manner. Clearly then, a nominal measure of gender does not signify whether males are superior or inferior to females. Numerical codes are often assigned to the values of nominal variables, adding to the confusion. For example, even though the value 1 is assigned for female and 2 for male, these are simply labels and no quantity or quality can be implied. No mathematical calculations can be applied to numbers that only serve as labels. Thus, limits are placed on what can and cannot be done statistically with these data. The most appropriate statistical measures for nominal data include: frequencies, proportions, probabilities and odds.

When the researcher goes beyond mere classification and seeks to assign order to cases in terms of the degree to which the subject has any given characteristic, he or she has assigned an *ordinal* level of measurement. With an ordinal scale, imagine a single continuum along which individuals may be ordered. However, the distances between values on the continuum may not always be meaningful or even known. Rather, the ordinal level of measurement yields information about the ordering of categories, but does not indicate the magnitude of differences between the numbers. An ordinal level of measurement supplies more information than is obtained using a nominal scale, since subjects are able to be grouped into separate categories, which can then be ordered. The order of the categories can be described by adjectives like more and less, bigger and smaller, stronger and weaker, etc. A familiar example of ordinal level of measurement is the classification of faculty as assistant, associate or full professors. Although we know a full professor is a higher status than an associate or assistant, it cannot be said that two associates equal one full professor.

Additionally, most Likert scales are considered to be ordinal level of measurement. On student surveys, Likert scales are often used to measure satisfaction with services or the extent of agreement with various statements. For example, students

may be asked to respond to the question, "Overall, how satisfied are you with the social life on campus?" on a 5-point scale where 1 equals 'very dissatisfied' and 5 equals 'very satisfied.' Clearly, if respondent A marks a 5 and respondent B marks a 4, then respondent A is more satisfied than respondent B. However, the magnitude of the difference in their levels of satisfaction is not directly distinguishable.

By contrast, *interval* level of measurement not only classifies according to the ordering of categories, but also indicates the exact distance between levels. The interval scale requires the establishment of some common standard unit of measurement that is accepted and replicable. Common examples of interval level of measurement are SAT scores and temperature in Fahrenheit or Celsius. Given a standard unit of measurement, it is possible to state that the difference between two subjects is a particular number of units. However with interval data, it is not possible to make direct ratio comparisons between levels of the data. With interval data such comparisons are not possible because there is no meaningful zero point (i.e., zero does not imply the absence of the quantity being measured). For example, 0 Celsius does not imply no temperature; rather the value represents the freezing point of water. Also, SAT scores are normally considered interval because the base is not equal to zero or "no ability." Thus, a score of 600 is not twice as high as a score of 300.

If it is possible to locate an absolute and non arbitrary zero point on the scale, then the data are *ratio*, the highest level of the measurement hierarchy. In this case, scores can be compared by using ratios. For example, if the endowment of school A is $10 million and the endowment of school B is $25 million, then school B's endowment can be said to be 2 ½ times that of school A. After all it is possible to have a $0 endowment. While many researchers make the distinction between interval and ratio level of measurement, some do not. Although the distinction between the two is subtle, it is important to recognize the limitation on the types of comparisons of scores one can make between the two levels. On the other hand, fewer statistical techniques require a ratio scale; making the distinction between the interval and ratio levels of measurement somewhat irrelevant.

All statistical analyses require a particular minimal level of measurement. An important general guideline is that statistics based on one level of measurement should not be used for a lower level, but can be used for a higher level. For example, statistics requiring ordinal data may be used on interval or ratio data, but should not be used on nominal data. Figures 1 and 2 summarize the characteristics of each of the four levels that have been discussed and illustrate the relationship of the levels of measurement of the variable to the level of measurement for statistical analysis. It is important to note that when a higher level of measurement of data is analyzed using a statistic based on a lower level of measurement, information may be lost if the data is collapsed into broader more discrete categories. Thus, the decisions made concerning the level of measurement of variables have a direct impact on the type of statistical analyses that can be performed.

To review the levels of measurement consider the following scenario: you are consulting with your admissions office on the design of an Inquiry Survey and you wish to add a question concerning income level. Figure 3 summarizes several adequate ways that you could ask for this information. Each of the four questions will result in one of the four levels of measurement. In deciding which question to use, a general rule of thumb is to measure at the highest level appropriate and possible. You can always collapse or combine scores later to create a lower level of

Figure 1

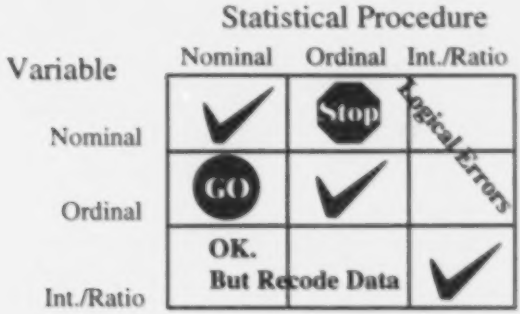
Summary of Levels of Measurement

Characteristics	Levels of Measurement: Nominal	Ordinal	Interval	Ratio
Mutually Exclusive	✓	✓	✓	✓
Order to Scale		✓	✓	✓
Standardized Scale			✓	✓
Meaningful Zero				✓

Note: Figure is the work of David Drews, Juanita College.

Figure 2

Relationship between Level of Measurement and Use of Statistical Procedures



Note: Statistical analyses are appropriate or not appropriate depending on the level of measurement of your data. Figure is the work of David Drews, Juanita College.

measurement; however, the reverse is not possible. Keep in mind, for some variables levels of measurement other than nominal or ordinal are not possible. For example, gender or ethnic background may only be nominal and most attitudinal scales are ordinal in nature.

Figure 3

Examples of Levels of Measurement

1. Do you work? ___Yes ___No [nominal]

2. Please indicate how you would classify your socio-economic status: [ordinal]

   ___low-income ___middle-income ___upper-income

3. Please check the category that appropriately describes your annual earnings: [interval]

   ___$0 to $25,000 ___$50,001 to $75,000

   ___$25,001 to $50,000 ___over $75,000

4. What was your annual income for last year? _____
   [ratio]

In general, statistical procedures may be grouped into two classifications: parametric or non-parametric. A major distinction between the two classifications is that parametric procedures require interval or ratio level of measurement, while non-parametric procedures only require nominal or ordinal measurement.[1] For the most part, the emphasis in this text will be on parametric procedures, with the exception of the Descriptive Statistics section of this chapter and Chapter 4 on Chi-Square.

Once a variable has been clearly defined and measured the researcher must consider the validity and reliability of measures as an important aspect of research design. Validity is the degree to which a test or scale measures what it purports to measure, while reliability is the extent to which a test or scale consistently measures what it purports to measure. Measures are said to be *reliable* when repeated trials yield similar results. For example, if your student information system yields a different count each time you request it, the system may not be considered to be reliable. Measures are said to be *valid* when they are indeed measuring what the researcher claims they are. By definition, measures that are valid are reliable; however, measures that are reliable may or may not be valid. For example, the SAT examination process has had its validity questioned as an achievement test. Some opponents claim it is a test of how successful SAT preparation courses are, while others claim it serves best as an indicator of parental income, socio-economic status, high school quality and race. Yet the score distributions are highly reliable across years.

This discussion of variable characteristics will end with the definition of independent and dependent variables. In statistical analyses, variables are referred to as being either *independent* or *dependent*. These terms define, in part, how the variables relate to one another. Some researchers use the terms *causal* or *predictor* as synonymous with *independent* and *resultant* or *criterion* with *dependent*. Variables are labeled as

---

[1] Also, parametric techniques make an assumption about the normal distribution of data and non-parametric do not. Both parametric and non-parametric statistics have both descriptive and inferential alternatives.

independent when we want to examine their influences on other variables. Variables are labeled as dependent when their values are used to measure the effects of the independent variable(s). In statistical models, the value of the dependent variable **depends**, in part, on the value of the independent variable(s). In some instances, variables can be used as either independent or dependent in any given analysis. For example, one researcher could examine the influences of gender on SAT performance. In this analysis, gender would be the independent variable and SAT the dependent. However, in another analysis, the influences of SAT and gender on college choice could be explored. In this analysis, both gender and SAT are independent variables and college choice would be the dependent measure. With this background, let us now turn our attention to the basic principles of descriptive statistics.

Descriptive Statistics

Descriptive statistics is familiar to most Institutional Researchers and is used primarily to *describe* important characteristics of data. Three common types of descriptive statistics are central scores or measures of central tendency, variation within the scores or measures of dispersion, and the nature or shape of the distribution.

Measures of Central Tendency. When summarizing data one of the first measures most individuals seek is a 'central' or 'average' score. An important and basic point to remember is that there are several different ways to compute an average. The *mean* is the arithmetic average of all scores and is the most overused and abused workhorse of all the measures of central tendency. When given a list of scores and asked to produce an average, most people will obligingly proceed first to total all the scores and then to divide that total by the number of scores. However the mean should only be applied when the data consist of an interval or ratio level of measurement and thus produce a parametric statistic, although it is common practice to use the mean as measure of central tendency with ordinal scales as well. For example, meaningful interpretation exists for the mean of a Likert scale (e.g. the mean of a rating of overall satisfaction of the college experience).

On the other hand, it is totally inappropriate to report the mean of categorical data. One would not report the average gender as 1.67, although this could be interpreted as implying that the distribution was mostly female (if male was coded 1 and female coded 2). If more than two categories existed, then all potentially decipherable meaning would be lost. In general, reporting the mean of a nominal scale is considered a statistical taboo.

The *median* is the middle value when the scores are arranged in order of increasing magnitude. A median can be used to describe ordinal, interval and ratio levels of data and is synonymous with the 50th percentile. The score representing the median is located at the point where 50 percent of the cases fall above and 50 percent fall below. As the definition states, the median may be found by arranging all responses in numerical order and locating the middle score. If the number of scores is an odd number, the median is the number that is exactly in the middle of the list, while if the number of scores is even, the median is found by computing the mean of the two middle values. For example, if you have 13 scores the median is the value of the 7th score, while if you have 14 scores the median is the mean of the 7th and 8th scores (Example Box 3).

Example Box 3

1, 2, 2, 3, 4, 5, 6, 7, 7, 8, 9, 10, 12	1, 2, 2, 3, 4, 5, 6, 7, 7, 8, 9, 10, 12, 19
Median = 7th score	Median is between the 7th & 8th scores
Median = 6	Median = 6.5

The *mode* of a set of scores is obtained by selecting the score that occurs most frequently. In instances where no score is repeated, no mode exists. In those cases when two scores both have the greatest frequency, the distribution is bi-modal and both values are listed as the mode. Also, if more than two scores occur with the same greatest frequency, the distribution is said to be multi-modal and each is listed as a mode. The mode is appropriately calculated with all levels of data, but is the only measure of central of tendency applicable for nominal level data. For interval and ratio scales the mode provides little information in comparison to the mean and median, although the mode can easily be calculated.

Technically either the mean, median or mode can be reported as a central tendency or "**average score**"; however, the freedom to select a particular statistic (i.e., mean, median, or mode) can slant the description of data. Consider an SAT distribution with a mean of 647, median of 660 and mode of 690. Reporting the mean presents a lower average SAT; the mode a higher average. So how does one decide which statistic to report? The level of measurement, distribution of data, and characteristic of the statistic must be taken into account. The mean is most affected by extreme scores. One extremely high or extremely low score can drastically alter the mean, while the median is a measure of position and is not affected by extreme scores. In contrast, the mode does not take all scores into consideration - only those occurring with the greatest frequency. In general, if data are of a ratio level of measurement and are not suspect to extreme scores, the mean would be the most appropriate statistic. Under those circumstances where extreme scores are plausible, the median should then be reported. When in doubt, report both. Finally, if data are nominal, the mode should be reported.

Measures of Dispersion. It is quite possible for two different sets of scores to have the same mean, median, and mode (Table 1). Yet a simple perusal of the data values would lead one to state that the data sets are not at all similar. So, what distinguishes these two distributions from one another? The manner in which the scores are distributed about their central scores is the distinguishing factor. Several statistical techniques describe the variability of scores (i.e., measures of dispersion). The range is the simplest of these measures and is the difference between the highest and lowest score. For example, if the lowest institutional grant given to a member of the incoming class is $500 and the highest award is $15,000, then the range of grant awards is $14,500.

Percentiles may also be used to tell where a score lies in relation to the rest of the distribution. Percentiles report the proportion of scores that fall below a given score. For example, if a student scored in the 88th percentile on the MCAT exams then she earned a higher score than 88 percent of students who took that exam. The most often used percentile is the 50th percentile (i.e., the median); yet, reviewing the median for the two data sets in Table 1 we find the same value. However, a set of percentiles may be used in a box and whisker format to provide a quick and

Table 1

Comparative Data Sets

Group A	Group B
65	42
66	54
67	58
68	62
71	67
73	77
74	77
77	85
77	93
77	100

SPSS Descriptive Statistics

GROUP_A Group A

Mean	71.500	Median	72.000	Mode	77.000
Std dev	4.767	Variance	22.722	Range	12.000

Percentile	Value	Percentile	Value	Percentile	Value
25.00	66.750	50.00	72.000	75.00	77.000

Valid cases 10 Missing cases 0

- -

GROUP_B Group B

Mean	71.500	Median	72.000	Mode	77.000
Std dev	18.216	Variance	331.833	Range	58.000

Percentile	Value	Percentile	Value	Percentile	Value
25.00	57.000	50.00	72.000	75.00	87.000

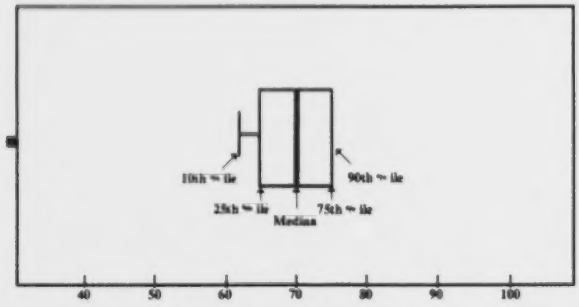
Valid cases 10 Missing cases 0

accurate image of the variability of the distribution. Techniques for creating box and whisker plots vary. Most involve the use of the 10th, 25th, 50th, 75th, and 90th percentiles. The standard graphical format for this plot includes: a horizontal scale representing the range of scores of data, a vertical line for the 50th percentile, a box around the middle 50 percent of the distribution (i.e., between the 25th and 75th percentiles) and extending whiskers to the 10th and 90th percentiles. Some box and whisker plots include other markers, such as points for the 1st and 99th percentiles. Figure 4 displays two box and whisker plots for the data sets found in Table 1. Notice how these plots graphically tell the differences in the distribution of these two data sets. Data set B has a much larger box indicating the greater spread in the scores than does data set A.

Figure 4

Box & Whisker Plots for Test Scores from Table 1

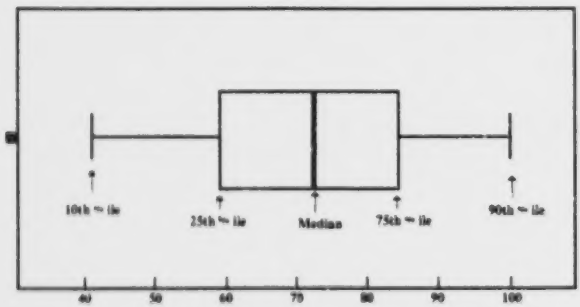
Group A



Test Scores

Note: In this data set the 75th and 90th percentiles are the same value.

Group B



Test Scores

Standard deviation and variance are two statistics that quantify the variability of scores about the mean of a distribution. Like the mean, these measures of variability should only be computed when data are interval or ratio level of measurement and thus are considered to be parametric statistics. First, one should clearly understand that standard deviation and variance measure the characteristics of dispersion or variation among the scores. Thus, scores grouped closer about their mean will yield a smaller standard deviation or variance. Notice in Table 1 that data set A has a smaller standard deviation and variance than set B. Conversely, as the data spread farther away from the mean the corresponding values of standard deviation and variance increase.

When measuring dispersion in a collection of data, one reasonable approach is to begin by determining the individual amounts by which scores deviate from the mean ($\bar{x}$). For any one score, the amount of deviation can be found by subtracting the score from the mean ($x - \bar{x}$). Logically, a good measure of dispersion would seem to be the sum of the deviations for all scores (i.e., $\Sigma(x-\bar{x})$); however, because the mean is the central score, this sum will always equal 0. One way to correct this problem is to square each of the deviations. So, in computational terms, variance can be determined by summing the squared value of deviation of each score from the mean, and divide that sum by the number of scores minus one (i.e., $\Sigma(x-\bar{x})^2/n-1$). Example Box 4 shows these calculations for data set A in Table 1.

Example Box 4

x	$x-\bar{x}$	$(x-\bar{x})^2$
65	-6.5	42.25
66	-5.5	30.25
67	-4.5	20.25
68	-3.5	12.25
71	-0.5	0.25
73	1.5	2.25
74	2.5	6.25
77	5.5	30.25
77	5.5	30.25
77	5.5	30.25
Sum = 715	Sum = 0	Sum = 206.5
Mean = 71.5		Variance = 22.722

Standard deviation is a simple algebraic manipulation of variance. To obtain standard deviation from variance, take the square root; vice versa, to obtain variance from standard deviation, square the value. The computational formula discussed above is theoretical in nature and is designed to illustrate the principles of standard deviation and variance; in practice, one would not use this formula to derive standard deviation or variance. Shorter computational formulas are available; better yet, use a statistical package.

Distribution Shape. When analyzing data one of the first steps that Institutional Researchers perform is to create frequency distributions. This first step allows one to get a first look at the data and provides *a feel for the data* to serve as a guide for future analyses. A frequency distribution is aptly named as it lists all the categories of scores in either ascending or descending order, along with their corresponding frequency. In most statistical packages, along with the frequency for each category, the percentage, valid percentage and cumulative percentage are presented. The percentage represents the percent of the total sample size that corresponded with that response. The valid percentage excludes respondents missing a value for that particular variable and cumulative percent summarizes the percentage included in the current and preceding responses. Cumulative percentages may be used to determine any percentile including the median. To determine the median from a frequency distribution, look down the cumulative percentage column for the first category that contains 50.0% or greater; the corresponding value for that category is the median. Table 2 presents a frequency distribution of SAT scores produced using SPSS.

While a frequency distribution presents a table that summarizes the shape of the distribution, graphics are frequently used to provide a visual image of the distribution shape. The distribution of data is an extremely important characteristic that affects the methods of analysis for and conclusion drawn from data. Statisticians have identified some common distribution shapes: uniform, bi-modal, multi-modal, positively-skewed, negatively-skewed, and normal. Figure 5 presents a graphic display of each of these distribution shapes. A distribution that is evenly spread over the range of possibilities is called uniform. In bi-modal and multi-modal distributions, clusters or grouping of scores occur about each mode. In a negatively-skewed distribution, the majority of respondents scored on the high end of the scale, while a few outliers pulled the tail of the distribution to the negative end. The term "skew" refers to the tail, so when you think of a negatively-skewed distribution remember the tail goes to the low end of the scale. Conversely, in a positively-skewed distribution, the majority of the scores fall on the low end of the scale and a few outlying high scores pull the tail to the positive end of the scale.

The *normal distribution* is an important concept in understanding statistics. The normal distribution is a theoretical construct based on an infinite number of cases. The area under the curve includes all elements or cases and the curve is symmetric about the center point. Therefore, the right side of the distribution represents half of the cases and the left side the other half. The area under the curve between any two points on the horizontal axis represents the percentages of cases that fall within that range. The principles of the normal distribution are directly applicable to the distribution of variables and are an integral part of sampling theory.

The world as we know it is normally distributed. This implies that for most of the

Table 2
SPSS FREQUENCIES Output

SAT SAT Score

Value Label	Value	Frequency	Percent	Valid Percent	Cum Percent
	250	1	.2	.2	.2
	270	3	.5	.5	.7
	310	5	.9	.9	1.6
	320	1	.2	.2	1.7
	340	2	.3	.3	2.1
	360	3	.5	.5	2.6
	370	3	.5	.5	3.1
	390	3	.5	.5	3.6
	400	4	.6	.7	4.3
	410	2	.3	.3	4.7
	420	3	.5	.5	5.2
	430	5	.8	.9	6.0
	440	7	1.1	1.2	7.2
	450	5	.8	.9	8.1
	460	12	1.9	2.1	10.2
	470	8	1.3	1.4	11.6
	480	17	2.7	2.9	14.5
	490	19	2.9	3.3	17.8
	500	18	2.8	3.1	20.9
	510	14	2.2	2.4	23.3
	520	26	4.1	4.5	27.8
	530	31	4.9	5.3	33.1
	540	18	2.8	3.1	36.2
	550	33	5.2	5.7	41.9
	560	27	4.3	4.7	46.6
	570	32	5.0	5.5	52.1
	580	27	4.3	4.7	56.7
	590	29	4.6	5.0	61.7
	600	31	4.9	5.3	67.1
	610	15	2.4	2.6	69.7
	620	26	4.1	4.5	74.1
	630	21	3.3	3.6	77.8
	640	21	3.3	3.6	81.4
	650	22	3.5	3.8	85.2
	660	13	2.0	2.2	87.4
	670	24	3.8	4.32	91.6
	680	14	2.2	2.4	94.0
	690	8	1.3	1.4	95.3
	700	13	2.0	2.2	97.6
	710	5	.8	.9	98.4
	720	4	.6	.7	99.1
	730	5	.8	.9	100.0
	0	55	8.7	Missing	
	Total	635	100.0	100.0	

Mean	566.669	Median	570.000	Mode	550.000
Std Dev	84.924	Variance	7212.122		

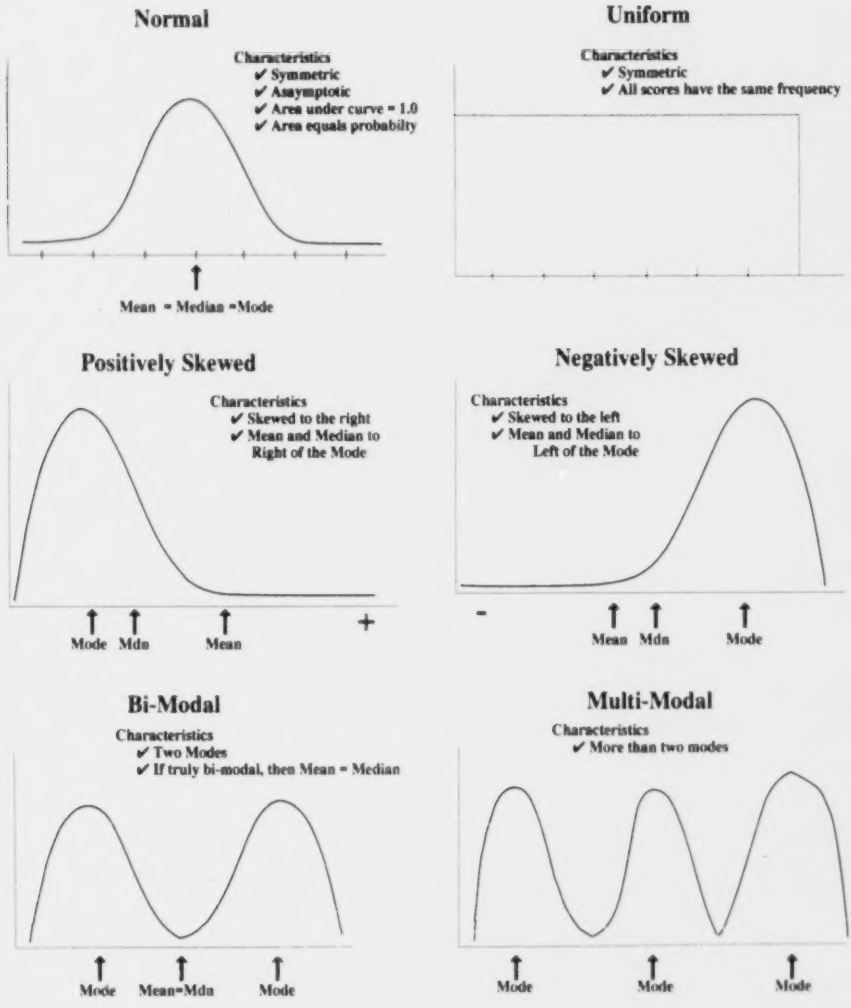
Percentile	Value	Percentile	Value	Percentile	Value
25.00	520.00	50.00	570.000	75.00	630.000

Valid cases 580 Missing cases 55

elements in the world that can be measured among large populations, few have very little of the element, most have some and few have a great deal. Let us consider intelligence (as measured by IQ). Very few people score below 75, most score around 110 and very few above 140 (Corsini, 1984). The normal distribution is graphically illustrated by a bell-shaped curve. The principle of normal distribution is also widely accepted as being applicable to a wide range of measurable characteristics, such as hand size, height, weight, number of free throws made, lung capacity, lifespan, and intelligence (just to name a few). The idea of characteristics being normally distributed in our world forms the foundation on which many statistical theories are based.

Figure 5

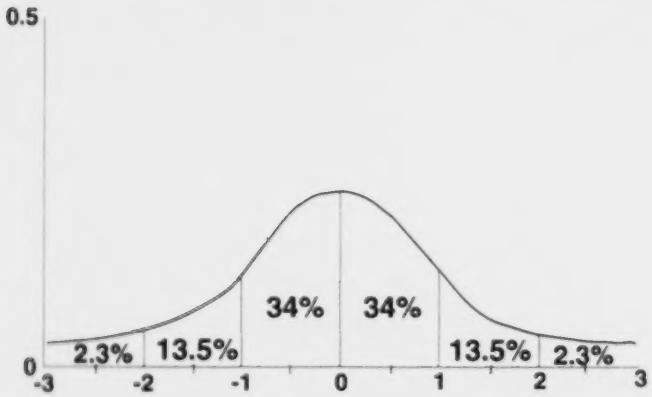
Distribution Shapes



If all elements in a normally-distributed theoretical population were measured and the population mean and standard deviation calculated, then 34 percent of the population would fall between the mean and one standard deviation above the mean and 34 percent would fall between the mean and one standard deviation below the mean. Thus, 68 percent of all elements would fall within one standard deviation of (above or below) the mean. An additional 13.5 percent would fall between the first and second standard

deviation from the mean; thus, 95 percent of all elements fall within 2 standard deviations of (above or below) the mean (34.0% + 34.0% + 13.5% + 13.5%). Next, another 2.3% falls between the second and third standard deviation from the mean; so 99.6 percent of all elements fall within 3 standard deviations of (above or below) the mean (34.0% + 34.0% + 13.5% + 13.5% + 2.3% + 2.3%). Finally, the remaining fraction of a percent is divided evenly between both the tails of the distribution beyond the third standard deviation. The percentages of the standard normal distribution are graphically displayed in Figure 6. In the real world, a surprisingly large number of variables when measured and plotted will create an essentially normal distribution.

Figure 6
The Standard Normal Distribution



Knowing what proportions of the curve fall within given standard deviations from the mean also provides knowledge about where the percentiles lie. If you know a score is one standard deviation above the mean, you also know that this score represents the 84th percentile. Why? Well, 50 percent of the distribution falls below the mean, then another 34 percent exists between the mean and 1 standard deviation above the mean, so 50 + 34 = 84. So if your score is 2 standard deviations above the mean, what percentile does that represent? Right, 97.5 (50 + 34 + 13.5).

In fact, the normal distribution is at the core of inferential statistics. In comparison to descriptive statistics, which describe important characteristics of data, inferential statistics allow us to make *inferences* and *draw conclusions* about a population based on sample data. Before discussing inferential statistics, it is crucial to define the terms *sample* and *population* and also understand the principles of probability, sampling theory, and the normal distribution.

Probability, Sampling Theory & the Normal Distribution

Probability theory and sampling are the basis for inferential statistics. In order to grasp an understanding of probability theory, the terms *sample* and *population* must be

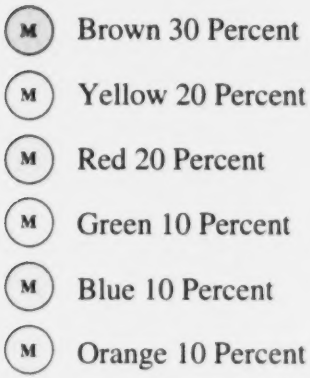
defined. A population consists of all elements or subjects to which your conclusions are intended to apply. A sample is a subset of the population that is actually measured and used as a matter of convenience. In probability we deal with a known population and make conclusions about a sample based on the knowledge of the population. For example, if the pool of applicants to an institution consists of 700 males and 800 females and we were to randomly select one applicant to receive an expense-paid visit to our institution, the chances of selecting a female are .53 or 800/1,500. Conversely in statistics, our population characteristics are unknown. First, make a random sample; next determine the sample statistic and then use the sample to make a conclusion about the population.

Thus, the sample is at the crux of inferential statistics. A sample is said to be random when every element has an equal and known chance of being included in the sample. No systematic or known bias can exist in a random sample. When surveying a sample of students on Campus Life issues, most Institutional Researchers draw a random sample of currently enrolled students, distribute the survey, collect responses and then assume that they have a true random sample. However, just because you have randomly selected subjects does not insure that you have a random sample of responses. In fact, rarely is a true random sample obtained in Institutional Research. For example, a 25 percent sample (2000 students) is randomly selected from the 8000 students enrolled at your university. A total of 1200 surveys are returned for a response rate of 60 percent. But, how can we know that no response bias is present in those who chose to complete and return the survey? Did only those students who were highly affiliated and satisfied with the institution respond, or is the opposite true? Did the respondent group exclude any portion of the population? For example, were off-campus students less likely to return the survey because it was delivered via campus mailboxes and they rarely check their boxes?

While most Institutional Researchers will verify the demographics of the non-respondent pool, the question still remains: Is the sample representative of the population? Well, the answer is not known, unless the entire population is measured. But sampling theory, properly applied, makes it highly likely that the sample is representative. A sample is drawn, because it is usually unreasonable to measure each member of the population (try to tell this to the Census Bureau). Remember, the intent is to measure a known portion of the population and to use that sample data to make inferences about the population. So if the sample is skewed does the model fall apart? **NO!** Although the representativeness of the sample may never be known, a degree of confidence regarding the extent to which a sample is representative of the population can be calculated. The sampling distribution of sample means allows us to determine this confidence interval. Now, let us explore this important principle with a theoretical example.

Sampling Distribution of Sample Means. This example is much more enjoyable if you have a box of M & M candies to follow along with us. The possibility of including a box with the text presented insurmountable logistical challenges. Now we know how M & M's are distributed. The Mars company in Hackettstown, New Jersey provided the distribution for plain M & M's reported in Figure 7. For your information, there are 519 plain candies per pound and 183 peanut candies.

Figure 7
Distribution of Plain M & M's



So if we took repeated samples of 50 plain M & M's, the average number of red candies should approach 10 candies (20%). How many red candies in your sample (don't eat the data yet!) What is the mean number of red candies among all of the samples drawn? The range? Any outliers? We won't always find 10 in every sample; often we will find slightly more or slightly less, but rarely many more or many less. Sampling theory tells us that we can be confident our sample lies within a certain margin of error (i.e., a confidence interval). This theorem states that 95 percent of samples we would take will be within two standard deviations of the true value.[2] Therefore, when you survey students and 73 percent of them state that they are satisfied with their overall academic experience, you can infer that this is representative of the population. You know that this value is within 2 standard deviations of the true population proportion. There is still a 5 percent chance that your sample is not within two standard deviations of the true value. Just as if you ended up with a sample of only 2 red M & M's, you would have had bad luck in drawing a sample that is not representative of the population. **Now, if you haven't already had the urge, start munching on your M & M's**.

For all statistical techniques, basic assumptions drive the statistical formulas and provide the guidelines for their application. Recall how it is nonsensical to calculate a mean for nominal level data. The assumptions for inferential statistics, though less obvious, are equally critical to the appropriate use of the statistical technique. Many researchers, naively or conveniently, forget to check the limitations of data. Also, it is

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[2] It is important to recognize that different samples produce different confidence intervals and in the long run 95 percent of those intervals contain the actual population parameter. It is incorrect to say that the population parameter has a 95 percent chance of falling within the limits of any confidence interval, but it is correct to state, in the long run, 95 percent of all samples collected will contain the population parameters within its limits.

tempting to use some of the more powerful statistical techniques when they are not appropriate. While you may be able to pass your results off on a less educated audience, predictions or decisions made from these analyses will be less forgiving.

In the chapters that follow, various inferential techniques will be discussed. Each chapter we will use a case study approach to describe an Institutional Research scenario, discuss the background and assumptions for the statistical procedure, suggest ways for reporting statistical findings and discuss implications for decision-making.

Chapter Two

Comparing Group Means: Are There Real Differences Between Average Faculty Salaries Across Departments?

Case Study:

Faculty salaries vary by many factors, some of which are logical, such as length of service, age, rank, and demands of the market. Others are less logical, and may be attributable to unfair covert mechanisms in an institution's salary system, such as paying lower salaries to women or members of less lucrative departments. In any situation involving differences in means, some of the difference is attributable to randomly-occurring factors. For example, if you were to attend a meeting of the AAUP and asked a group of 1000 professors to randomly split into two groups and then you calculated the average salary for each of the two groups, you would not find that the two means are identical. In fact you could repeat this exercise 100 times and you would continue to find differences of varying sizes. Assuming that the two groups are created randomly, these differences are attributable to randomly occurring factors. The statistical procedures t-test, one-way Analysis of Variance (ANOVA) and Factorial ANOVA can be used to explore differences in means across groups. These tests help us decide whether a sample difference is real or the result of randomly-occurring factors. The procedures evaluate the magnitude of sample differences to determine whether the difference is merely the result of randomly-occurring factors, or if it is attributable to some other forces in the data (i.e., the independent variable(s)).

The case at hand involves the average faculty salaries at a small university. The chair of the Humanities division has learned that the average salary for assistant professors in her department is much lower than the average salary for assistant professors in the Business School. The Humanities chair fears that this may be reflective of a shift in the priorities of the university. Perhaps the university is de-emphasizing its traditional commitment to the liberal arts and is moving toward a pre-professional orientation. The chair wants to know if the magnitude of the difference between the average salaries of Humanities and Business assistant professors is large enough to attribute it to more than common or randomly occurring differences between the two groups. In the course of investigating the situation, the Humanities chair learns that the average salary for assistant professors in the Natural Sciences is also higher than for the Humanities. At first glance, this seems to further confirm her notion that the university is moving towards a pre-professional orientation. She now wants to know whether the Natural Science salaries differ significantly from those in the Humanities.

After a meeting of the Humanities faculty, a female assistant professor asks the chair to explain the large disparity between her salary two years into her job and the salary of her male colleague who teaches in the Natural Sciences with the same length of service. She wants to know if the university is perpetuating the national trend of paying women less than men for the same job. Many comparisons are possible and many questions may be answered that have legal, morale, and budgetary consequences for this university. The Institutional Research office is asked to investigate the disparities between

the salaries of assistant professors in the Humanities, Natural Sciences, and School of Business. This case study will be used to illustrate the application of the t-test and one-way ANOVA. The determination of which statistical procedure is most appropriate is dependent on the research design. Before proceeding with a brief discussion of research designs, some descriptive statistics for this case study are presented in Table 3.

Research Designs:

ANalysis Of VAriance (ANOVA) is a name for a collection of statistical models and methods that deal with whether or not the variable means differ significantly across observation groups. In general terms, ANOVA is a statistical method that permits one to make an interpretive statement about overall differences among the means for the groups of observations. ANOVA designs vary based on two elements. First, is the independent variable an **independent groups** or a **repeated measures** factor? Do not get the terms independent variable and independent groups confused. Remember in Chapter 1 we defined the term independent variable as the variable whose effects on the dependent variable we are attempting to measure. In an **independent groups** design, subjects are categorized into one and only one level of the independent variables. Probably, the most common example of an independent groups variable is gender. In a **repeated measures** design, all subjects are tested on all levels of the independent variable. In Institutional Research, tracking students over their years at our institution would be an example of a repeated measures variable (year in school). In basic terms, **independent groups** refers to measuring different groups of people usually at the same time and **repeated measures**, the same people measured at different times. The simpler of the two forms from a calculation or interpretive viewpoint is the **independent groups** design. In contrast to the **independent groups** design, the **repeated measures** design has greater face validity in that the subjects are being compared to themselves.

The second element in determining design is only relevant to ANOVA. This element is the number of independent variables. By contrast, a t-test may only have one independent variable, which has only two levels. A t-test is nothing more than a special case of ANOVA in which the one independent variable has only two levels. A one-way ANOVA may only have one independent variable, but this variable has three or more levels. Comparing the GPAs of males to females would be an example of an independent groups t-test. Tracking the GPAs of students across their four years at our institution would be a one-way repeated measures ANOVA.

A Factorial ANOVA is an ANOVA that has any number of factors (i.e., independent variables) each with any number of levels (i.e., two or more). In each of these designs, the independent variable(s) may be either **independent groups** or **repeated measures** factors, leaving an inordinate amount of possible designs. For example, one might have a 2 X 4 ANOVA, the first factor being an **independent groups** factor with two levels representing the gender of a subject and the second variable being a **repeated measures** factor representing the GPA of a graduating senior at the end of each of his or her four years. This design is graphically illustrated in Example Box 5 and would be referred to as a mixed Factorial ANOVA.

Table 3

Descriptive Statistics for Salary Data of

Assistant Professors across Gender and Division

Division	Female			Male			Overall		
	M	SD	N	M	SD	N	M	SD	N
Humanities	49,838.52	9,224.04	24	45,796.33	8,719.61	24	48,736.10	9,138.01	48
Natural Sciences	56,365.24	6,898.76	21	54,213.14	5,871.54	28	55,135.47	6,354.56	49
Business	61,250.00	9,148.08	3	59,424.77	7,754.28	15	59,728.97	7,736.50	18
Overall	53,407.17	8,932.45	48	54,259.74	8,195.85	67	53,850.51	8,824.46	115

Example Box 5

	First-Year	Sophomore	Junior	Senior
Female	GPA	➪	➪	➪
Male	GPA	➪	➪	➪

Throughout the remainder of this chapter, we will discuss two statistical procedures that could be applied to our case study: a t-test comparing male and female salaries, and a one-way ANOVA comparing faculty salary across the three divisions. In each of these analyses the independent variable(s) are independent groups factors, as faculty are either male or female and are associated with only one department. It is important to note that an independent groups Factorial ANOVA is the most appropriate design for this research question. The explanation for this point will be documented throughout the remainder of the discussion. However, let's back up and start with the more familiar descriptive statistics and t-test procedures.

Analysis of Data:

In the above described case study, our department chair has begun the process of exploring the descriptive statistics of faculty salary data. Table 3 contains the mean, standard deviation and sample size for the salaries of male and female assistant professors in the Humanities, Natural Sciences, and School of Business. The overall mean for assistant professors is $53,850.51 with a standard deviation of $8,824.46. Female assistant professors in the Business School have the highest mean salary ($\bar{x}$ = 61,250) of all the subgroups. However, there are only 3 female assistant professors in the Business department. From our previous discussion of measures of central tendencies, we are aware that we must probe deeper than a simple examination of the group means. As is evident from this discussion, we are still left with the same basic questions defined in our case study. Are these differences meaningful or can they be attributed to randomly-occurring factors? To answer this question we must use inferential statistical techniques. Inferential statistical procedures allow us to draw conclusions about a population based upon sample data.

T-TEST

A basic question of our case study is whether or not there are differences in the salaries of male and female assistant professors. In other words, is the university perpetuating the national trend of paying women less than men for the same job? In essence the answer to that question lies in the comparison between the mean salary for male ($\bar{x}$ = 54,259.74) and female ($\bar{x}$ = 53,407.18) assistant professors. Certainly the average salary for male assistant professors is higher than the mean for females, but is the magnitude of the difference between the two means significant enough to be attributed to gender bias? Otherwise, the difference will be attributed to randomly-occurring factors. The calculation and interpretation of an independent groups t-test comparing male and female salaries will answer this question. Before calculating and interpreting this statistic, let's review the basic assumptions of the t-test.

Background & Basic Assumptions

A t-test determines whether the difference between two group means is likely to have occurred by chance or whether the difference is attributable to the levels (or groups) of the independent variable. In order to calculate a t-test, the research design must contain only one dependent variable (in this case, salary) measured on an interval or ratio scale and one independent variable which has only two levels (in this case, gender). The independent variable may either be an independent groups or repeated measures factor (in this case, independent groups). Thus there are two versions of the t-test: independent groups and repeated measures.[1]

Another assumption of the independent groups t-test is that the scores within each level of the independent variable are independent of one another. In our analysis and most applications, independent observations are assumed when each subject supplies only one score. However, when an independent groups design is used, the population characteristics of the two distributions may be quite different. The t-test uses the assumption of homogeneity of variance which states that the variances of the two levels of the independent variable must be equal. Remember in Chapter 1, an illustration was provided where the measures of central tendency for two samples were the same, yet the dispersion of the scores was quite different. In this case if we were comparing the means of these two groups we might have violated this assumption. Numerous tests are available for evaluating this assumption. SPSS calculates the Levene test of homogeneity of variance. Norusis (1993) described this procedure as "less dependent on the assumption of normality than most tests" (p. 187). The null hypothesis for this test is that the groups (i.e., levels of the independent variable) come from populations with equal variances. The Levene statistic is an F ratio and interpretation of the significance of the F value will determine whether you have met or violated the assumption.[2] In lieu of this or other tests, Grimm (1993) suggested the following rule of thumb to evaluate this assumption: "Examine the sample variances: if one of them is four times larger than the other, you will probably violate the assumption" (p. 182).

Overall, the t-test is a robust test. This implies that the test is not always adversely affected when one of the assumptions has been violated, particularly if the two sample sizes (i.e., the levels of the independent variable) are equivalent ($n_1 = n_2$) and the overall sample size is large ($N > 30$) (Grimm, 1993; Triola, 1992). Yet these assumptions should not be ignored. In fact the discovery that the variances between the two groups are significantly different from one another can be an interesting finding, even if the means of the two groups are not significantly different. If the assumption of homogeneity of

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[1] Some texts and software packages refer to independent groups as independent samples and repeated measures as dependent samples, paired samples, or correlated samples.

[2] Thus, non significance equates to meeting the assumption of homogeneity of variance and significance indicates a violation of the assumption.

variance has been violated, there is a statistical adjustment to the t-test formula, which is reported by most statistical software packages, including SPSS. In SPSS, the equal variances t-test is used with homogenous variances, and the unequal variances t-test for heterogeneous variances. Finally, if the group sample sizes are not equivalent, the overall sample size is small, or one or more of the assumptions has been violated, a test of significance that does not make assumptions about the population distributions should be used. These tests are referred to as non-parametric tests. A discussion of equivalent non-parametric statistics appears at the conclusion of this chapter.

T-Test Analysis:

In this analysis, the dollar amount of the annual salary of assistant professors will be used as the dependent variable. The independent variable gender is an independent groups factor with two levels: male and female. An independent groups t-test was calculated comparing the mean salary for male and female assistant professors. The T-TEST procedure from SPSS (Norusis, 1993) was used to calculate this statistic. The output from this t-test procedure may be found in Table 4.

In reviewing the output in Table 4, Levene's test of equality of the variances indicates that the assumption of homogeneity of variance has been met, since the $p > .05$. Therefore, the t-test formula that should be interpreted is labeled for equal variances. The t- test (-.50) is calculated by dividing the mean difference[1] (-852.5654) by the standard error of the difference (1712.777) labeled SE of DIFF on the printout. The significance of the t-test was reported as .620. Since this value is clearly greater than the normal alpha level of .05, we must conclude that no significant difference exists between the means of the male and female assistant professors. Although a difference exists between the mean *sample* salaries of male ($\bar{x}$ = 54,259.74) and female ($\bar{x}$ = 53,407.18) assistant professors, this difference is not large enough to be attributed to anything more than random occurrences.

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[1] In the calculation of the t-test, SPSS always subtracts the mean of the group coded 2 from the mean of the group coded 1. The negative mean difference was created because females were coded as 1 and have a lower mean than the males who were coded 2. Thus, a negative mean difference indicates that the second group has a higher mean than the group coded 1.

Table 4

SPSS Output from t-tests for

Independent Samples of GENDER

Variable	Number of Cases	Mean	SD	SE of Mean
SALARY				
Female	48	53407.1750	8932.451	1289.288
Male	52	54259.7404	8195.847	1136.560

Mean Difference = -852.5654

Levene's Test for Equality of Variances: F= .631 P= .429

t-test for Equality of Means Variances	t-value	df	2-Tail Sig	SE of Diff	95% CI for Diff
Equal	-.50	98	620	1712.777	(-4252.28, 2547.148)
Unequal	-.50	95.36	621	1718.730	(-4265.44, 2560.310)

Thus, we can refute the claim that the university is perpetuating the national trend of paying women less than men for the same job.

One-way ANOVA

The next basic question of our case study is whether or not there are differences between the mean salaries of assistant professors in the humanities ($\bar{x}$ = 48,736.10), natural sciences ($\bar{x}$ = 55,135.47) and business ($\bar{x}$ = 59,728.97) divisions. Again, the answer to this question is found through a comparison of these three means. Certainly, a large difference exists between the average salary for assistant professors in the humanities and business divisions, and less of a difference between the natural sciences and business, and humanities and natural sciences. However, to establish what is a large enough difference to be attributed to a shift in priorities within the institution, we must apply inferential statistics. The calculation and interpretation of a one-way independent groups ANOVA will answer this question. Before calculating and interpreting this statistic, the basic assumptions of the one-way ANOVA will be reviewed.

Background & Basic Assumptions:

As was illustrated, t-test is a common statistical procedure used to test the difference between the means of just two groups. ANOVA allows comparison among more than two sample means. One-way ANOVA deals with a single categorical independent variable (or factor). In order to perform a one-way ANOVA, the research

design must contain only one dependent variable measured on an interval or ratio scale. The independent variable is used to classify subjects or observations into separate categories or groups. The research design for the one-way ANOVA must contain only one independent variable and that variable should have three or more levels.[4]

Often individuals ask if they can perform multiple t-tests to make the paired comparisons between the levels of the independent variable instead of a one-way ANOVA.[5] Given that a t-test is a special case of ANOVA in which the independent variable has only two levels and that the squared t-value (t^2) is equivalent to the F-ratio for determining statistical significance between two groups using ANOVA, there would seem to be logical basis for such a procedure. However, this procedure **is *not* statistically appropriate**. The use of multiple t-tests leads to a loss of any interpretable level of significance (i.e., alpha (27) level). In ANOVA, the alpha level is used to make decisions regarding statistical significance of the differences between the group means. Thus, when the alpha level is set at .05 and a t-test is conducted, there is a probability of making an error by stating that differences existed between the group means, when in reality they did not differ. The probability of this type of error for that one test is 5 percent. When a series of t-tests is run, the probability of mistakenly stating that differences existed is inflated. In fact, Grimm (1993) stated that if three t-tests are performed, as in our case study, a .05 alpha level would be inflated to .14 and if 10 tests were performed the same alpha (.05) would be inflated to .40. Thus, you would have a 40 percent chance of finding differences that look real, but in fact are due to random occurrences.

From a statistical viewpoint, the same three assumptions that were appropriate for the independent groups t-test are appropriate for the one-way independent groups ANOVA. First, the dependent variable must come from an essentially normally-distributed population. Second, the scores within each level of the independent variable are assumed to be independent of one another. This assumption of independent observations is only appropriate for an independent groups analysis and is assumed through the research design. Finally, the variance of the dependent measure should be essentially constant for all categories or groups of the independent variables. A term for this second assumption, if met, is homogeneity of variance. Again, SPSS calculates the Levene test of equality of variances to check this assumption. Unlike the t-test, if this assumption is violated, no statistical adjustment can be made. Therefore the researcher would determine which variances are distinctly different, report the violation, and proceed with the ANOVA procedure assuming that the test was robust.

---

[4] If there are only two levels to the independent variable then a t-test would be run. Also, if there is more than one independent variable then a factorial ANOVA would be more appropriate.

[5] In our example this would be equivalent to running three t-tests; comparing: Humanities versus Business, Humanities versus Natural Sciences, and Natural Sciences versus Business.

The calculation of the ANOVA centers around the calculation of the F-ratio. In basic terms, the F-ratio is computed as follows:

$$F = \frac{\text{variance between groups}}{\text{variance within groups}}$$

This computation requires the calculation of three sources of variance (sum of squares, [SS]): between groups, within groups, and total. These three sources can best be seen graphically in Figure 8. Each of these sources of variance has degrees of freedom associated with it. Degrees of freedom are adjustments that are made to sources of variation based on either sample size or the number of levels in the independent variable or both. The mean square (MS) of the variance between and within samples is equivalent to the sum of squares (SS) between and within groups divided by its associated degrees of freedom. The calculations of the one-way ANOVA can best be summarized in the common table format displayed in Table 5.

Figure 8

ANOVA Sources of Variation

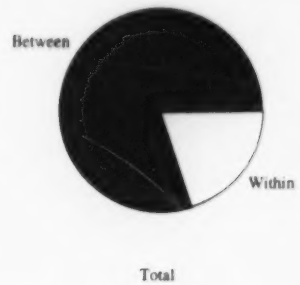

Table 5
Summary Table for ONE-WAY ANOVA

SOURCE	SS	df	MS	F	p
Between Groups	SS_B	k-1	SS_B/df_B	MS_B/MS_W	
Within Groups	SS_W	N-k	SS_W/df_W		
Total		N-1			

Note: K represents the number of levels of the independent variable and N, the total sample size.

The F-ratio directly addresses the hypothesis as to whether or not the means differ across observation groups (i.e., levels of the independent variable). In generic form, the null (H_0) and alternative hypotheses (H_1) could be stated as follows:

H_o: All the means are equal.
H_1: At least two of the means are different[6]

If the F-ratio is non-significant, we accept the Null hypothesis (Ho), and our analysis is completed by reporting that no significant differences exist among the three means. But if the F-value is significant, then there are a number of procedures called post-hoc comparisons or multiple range tests that are used to find out where the significant differences lie. For example, are the differences between Humanities and Business, Business and Natural Sciences, Natural Sciences and Humanities, or all three?

The use of a t-test for post-hoc comparisons is still not statistically appropriate because the same problem that we discussed earlier with the alpha level still exists. Appropriate methods include Newman-Kuels, Tukey's Honest Significant Difference, Scheffé, and several others. Each of the tests is calculated in a slightly different manner and is conceptually different from the others in their treatment of alpha. The Scheffé method is the most conservative, which means that it identifies fewer significant differences. Newman-Kuels is more liberal, identifying more significant differences, and Tukey's falls between the other two. Let us now turn to an analysis of our case study data to illustrate these post-hoc comparisons methods.

One-way ANOVA Analysis:

From our case study example, we will examine the salary of assistant professors based on the division to which they are assigned. Our example has three divisions: Humanities, Natural Sciences, and Business. All assistant professors are affiliated with only one division; thus our design is a one-way ANOVA with one independent groups factor (i.e., division). The dependent variable for this analysis is the dollar amount of the annual salary of the assistant professors. The ONEWAY procedure from SPSS (Norusis, 1993) was used to calculate the F-test statistic. The output may be found in Table 6.

In reviewing the output in Table 6, the Levene test for the assumption of homogeneity of variances indicates that this assumption has been met with $p > .05$. Notice that the SPSS output follows the common ANOVA table format described above. The significance of the calculated F ratio (13.4964), labeled F Prob., was .000, indicating that a significant difference exists between the mean salaries of assistant professors across

---

[6] Commonly researchers describe the alternative hypothesis as *all of the means are not equal*. However, Grimm (1993) indicates that this wording is technically incorrect, due to the fact that a significant difference between only two means will result in the rejection of the null hypothesis. Thus, the wording *at least two of the means are different* is recommended to represent H_1.

the three divisions (i.e., Humanities, Natural Sciences, & Business). While this finding indicates that there is a very small chance that the differences in the mean salaries occurred just by chance, and that an explanation other than random differences must be considered, it does not identify specifically where the differences are found. To answer this question, post

Table 6

SPSS Output from the One-way ANOVA

Comparing Salary by Division

```
- - - - - O N E W A Y - - - - -

   Variable Salary
By Variable Division

                    Analysis of Variance

    Source          D.F.      Sum of Squares      Mean Squares      F Ratio      F Prob.

Between Groups         2      1566104872          783052436.0       13.50        .0000
Within Groups         97      5627873169          58019311.02
Total                 99      7193978041


Levene Test for Homogeneity of Variances

  Statistic    df1        df2        2-tail Sig.
  1.3380       2          97             267
```

hoc multiple comparisons tests must be run. To illustrate the similarities and differences between the various forms of multiple comparisons procedures, three different multiple range tests were run simultaneously on these data: Student Newman Kuels, Tukey's , and Scheffé. The SPSS output reporting the results of these procedures is found in Table 7. To interpret this output refer to the chart with the asterisks. The asterisks (*) indicate where significant differences have been found. When reporting the findings you must refer to your coding scheme for the independent variable. In our analysis, Humanities was coded 1, Natural Sciences - 2, and Business - 3.

Using our case study data, the Student Newman Kuels and the Tukey's-B procedures yield the same findings. Interpretation of these analyses indicate that the salaries for assistant professors across all divisions are significantly different from each other. Assistant professors in the Business division are paid the most, followed by Natural

Table 7
SPSS Output from the Multiple Range Post Hoc Comparisons

```
Multiple Range Tests:  Student-Newman-Keuls test significance level  .050

The difference between two means is significant if
  MEAN (J) -Mean (I)    >= 5386.0612  * RANGE *  SQRT (1/N(I)  +  1/N(J) )
  with the following value (s) for RANGE:

  Step      2         3
  RANGE    2.82      3.37

(*)  Indicates significant differences which are shown in the lower triangle

                          G   G   G
                          r   r   r
                          p   p   p

                          1   2   3
Mean              DEPT

 48736.1030       Grp 1
554135.4694       Grp 2   *
 59728.9722       Grp 3   *   *

Multiple Range Tests:  Tukey-B test with significance level  .050

The difference between two means is significant if
  MEAN (J) -MEAN (I)    >= 5386.0612  * RANGE *  SQRT(1/N (I)  +  1/N (J) )
  with the following value (s) for RANGE:

  Step      2         3
  RANGE    3.09      3.37

(*) Indicates significant differences which are shown in the lower triangle

                          G   G   G
                          r   r   r
                          p   p   p

                          1   2   3
Mean              DEPT

 48736.1030       Grp 1
554135.4694       Grp 2   *
 59728.9722       Grp 3   *   *

Multiple Range Tests:  Scheffe test with significance level  .05

The difference between two means is significant if
  MEAN (J) -MEAN (I)    >= 5386.0612  * RANGE *  SQRT(1/N (I)  +  1/N (J) )
  with the following value (s) for RANGE:  3.52

  Step      2         3
  RANGE    3.09      3.37

(*) Indicates significant differences which are shown in the lower triangle

                          G   G   G
                          r   r   r
                          p   p   p

                          1   2   3
Mean              DEPT

 48736.1030       Grp 1
554135.4694       Grp 2   *
 59728.9722       Grp 3   *
```

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Sciences, and then Humanities. However, when interpreting output from the more conservative procedure, Scheffé, the mean salary for assistant professors in the Humanities division was found to be significantly lower than either the Business or Natural Sciences divisions, but no significant difference was found between the Business and Natural Sciences divisions. Given the discrepancy between these procedures the researcher has a dilemma: which findings should be reported? Even though both the liberal (Student Newman Kuels) and moderate (Tukey's B) procedures replicate each other's findings, in this instance erring on the side of conservatism might be wise, given the sensitive nature of the topic. Thus, the results of the Scheffé procedure are probably more appropriate to report. No matter what analysis is reported, this is disturbing news for the institution. Certainly one possible interpretation of these findings is the claim of the chair of the Humanities division that the institution is de-emphasizing its traditional commitment to the liberal arts and is moving toward a pre-professional orientation. Since faculty salaries may vary based on many factors, the researcher should be more complete and thorough in exploring all possible interpretations. A model with only one explanatory (i.e., independent) variable is certainly not comprehensive, and further analysis and investigation is definitely warranted. Some other factors to consider in salary equity studies are length of service, years since Ph.D., Ph.D. origin, and number of publications.

Other Statistical Procedures for Comparing Group Means

To this point in our analysis of the case study data, we have found no differences in the salary of assistant professors based on gender and found significant differences between salaries across the three divisions. Yet several questions remain unanswered. Do gender and division interact with each other with regard to salary? Are there other independent variables, such as length of service, which should be included when examining differences in faculty salaries? For our purposes, in reviewing basic statistical procedures we have proceeded as far as the limits of this text will allow. However, basic descriptions of other statistical procedures that may be used to compare group means are presented to acquaint you with some of the more advanced designs.

Factorial ANOVA:

As was illustrated, the t-test allows comparison between two group means, while the one-way ANOVA has an advantage over a t-test: being able to make comparisons among more than two sample means from one independent variable. A factorial ANOVA is used when the research design includes more than one independent variable, each with any number of levels (i.e., two or more). Thus, factorial ANOVAs have an inordinate number of possible designs. Further, all factorial ANOVA models are labeled by the number of levels in each of the independent variables. A logical progression from our case study would be to extend the previous one-way ANOVA and add an additional independent variable that represents the gender of the professor. This particular factorial ANOVA is labeled as a 2 X 3 with two independent groups factors (i.e., gender - 2 levels and division - 3 levels). In our case study, this analysis may have been the most logical and appropriate statistical technique to calculate with the exception of one limitation, the

sample sizes. If you refer back to Table 3, you will be reminded of the fact that the sample sizes between the genders in each division was quite discrepant. For example, the number of female Business faculty was 3, while the number of female Natural Science faculty was 21. This small 'cell size' is problematic to the calculation of this ANOVA. As a result, collapsing to a 2 X 2 ANOVA by dropping the Business department would be recommended. A factorial ANOVA allows the researcher to test the impact of two different portions of the design, the **main effects** and the **interaction**. The **main effects** in a factorial design are similar to the univariate tests we just calculated. For our case study, the **main effects** would compare the impact of gender and division on the salary of assistant professors. The **interaction** or differential effect tests to determine if a different outcome is present across one or more levels of the two independent variables. Hence, the name interaction; do the two independent variables interact? For example, do female Business professors make more than male Humanities professors? Often, this question is the more interesting and most relevant to our research. In our case study, the analysis of the interaction would examine whether or not significant salary differences exist between male and female faculty members in each of the three divisions. In other words, does a differential effect exist between gender and division with regard to salary?

Analysis of Covariance (ANCOVA):

Analysis of Covariance is really an advanced form of ANOVA. An attempt will be made to describe a rather complex statistical procedure in rather basic terms. ANOVA procedures are grounded in linear regression. However, the procedure does not attempt to measure the fit between variables; rather, it seeks to determine the probability that a predictor variable could yield results different from simple random selection (Iverson & Norpoth, 1976). ANCOVA is an extension of the linear model for ANOVA. The most common application of ANCOVA is to examine the relationship between a continuous dependent variable and a categorical independent variable while controlling for the effects of a second continuous variable (i.e., nuisance variable). In essence, ANCOVA examines differences in the dependent variable among categories of the independent variable controlling for differences in the nuisance variable (covariate). For example, in institutional research it may be interesting to see differences in SAT scores between the genders after controlling for the level of IQ of the student. In our case study, we could control for the number of years of teaching. Years of experience is a variable that should be partialled out of salary in order to more effectively compare mean salaries.

While ANCOVA is generally highly regarded as a means of improving research design, one must be careful to ensure that ANCOVA is best suited to your study. When deciding whether or not to include a covariate, two questions must be considered. First, does a strong relationship exist between the covariate and the dependent measure ($r = .40$ or greater)? Second, is there little to no relationship between the covariate and the independent variable? In order for this analysis to be appropriate the answer to both of these questions must be yes. In order to warrant the partialing out of the impact of this nuisance variable (covariate), a strong relationship must exist between the covariate and the dependent variable. However, if a relationship exists between the covariate and the independent variable, then it becomes impossible to remove the effects of the covariate

from the analysis. Another word of caution: using a covariate is not necessarily the best method for dealing with differences in a known group. From a research design standpoint, it is far better to randomly assign subjects, if possible. Remember, **Garbage in, Garbage out**; no statistical procedure can save an inferior research design.

Multivariate ANalysis Of VAriance (MANOVA):

ANOVA is used to allow comparisons of a single dependent measure among two or more levels of an independent variable or variables. MANOVA is used when there is more than one dependent variable, and it is inappropriate to do a series of univariate tests. Again, please be reminded that the MANOVA procedure is an advanced and complex statistical procedure. Only a brief description of the purpose of this statistical procedure will be explored.

Two major reasons exist for performing a MANOVA as opposed to several univariate ANOVAs for each dependent variable. First, we often have several tests that are designed to measure various aspects of one overlying factor. For example, math and verbal SAT scores are both measures of a high school student's academic achievement. In other words, math and verbal SAT scores are often highly correlated; hence, if you find a significant difference between groups on math SAT you would most likely find one for verbal SAT. Testing both separately with univariate statistics is not the best approach because the two analyses are not independent. Secondly, the MANOVA procedure provides the researcher with the ability to study the interaction among the dependent variables. Just as the interaction among independent variables in a factorial ANOVA provides new information, which could not be uncovered by calculating separate tests, looking at two or more dependent variables simultaneously in a MANOVA provides more information than doing a series of univariate analyses.

Non-parametric Tests of Mean Differences:

When a researcher has violated the assumptions of parametric statistics, several non-parametric equivalent tests exist for comparing group means. Within the context of this text no attempt will be made to review all of these non-parametric procedures; rather a brief description of these procedures will be provided with sources of reference for further information. Within the context of Institutional Research, non-parametric statistics are often warranted because of the use of ordinal Likert scales on many of our survey instruments.

The non-parametric equivalent of the independent groups t-test is the Mann Whitney U test. The Wilcoxon Signed Rank test is the equivalent non-parametric measure for the repeated measures or paired t-test. Instead of the one-way independent groups ANOVA, a researcher should utilize the Kruskal Wallis test under non-parametric conditions. Finally, the non-parametric equivalent for the one-way ANOVA with repeated or dependent samples is the Friedman's ANOVA by Ranks procedure. No equivalent non-parametric procedures exist for Factorial ANOVA, ANCOVA, or MANOVA. Most basic statistical texts (e.g., Grimm, 1993; Triola, 1994) provide documentation on these basic

non-parametric statistics. For a more complete reference for non-parametric statistics, refer to Conover (1980), Mostella and Rourke (1973) or Siegal (1956).

Chapter Three

Correlation: Measuring the Relationship Between SAT and First-Year GPA

Case Study:

Each year admissions officers struggle to recruit qualified students for enrollment to institutions of higher education. At the same time, faculty may be questioning the quality of entering first-year students. Often admissions personnel are at a loss to determine those qualities that are most indicative of success at their institution. Historically, SAT scores have not shown strong predictive validity for first-year grade point average at many institutions. High school grade point average and admissions ratings have shown stronger associations with academic performance. Yet many institutions have found the need to rely more heavily on qualitative data, such as recommendations, essays, and interviews. Of course, the analysis of qualitative data is much more subjective, time consuming and costly than quantitative data.

The case at hand involves a private college with a variety of undergraduate programs centered around a basic liberal arts orientation. Recently, the faculty have raised questions about admissions standards and the quality of entering students. Faculty concerns are centered on decreasing academic performance. Many faculty fear the time has come to adjust the curriculum or a higher percentage of students will be receiving lower grades. The Director of Admissions has asked for your assistance in determining what are the best quantitative measures available to admissions officers for assessing the potential for academic success within the current curriculum.

The focus of this case study is to examine the 63[illegible] students who recently completed their first year at this institution and determine those variables in the admissions file that are most strongly related to academic success. From the student academic data base academic success is defined as the life-to-date grade point average (LTDGPA) of these students who recently completed their first year. From the admissions file, quantitative measures for these students are extracted and matched to their LTDGPA. These quantitative measures include: high school grade point average, verbal SAT, and math SAT. This case study will be used to illustrate the application of correlational analyses to measure the relationships among these variables.

Background:

A correlation coefficient measures the strength and direction of the linear relationship between two variables. Correlational procedures measure how one variable changes in relation to another. Examples in Institutional Research might include measuring the relationship between the size of the endowment of a college and the number of alumni, or the amount of money a college spends on recruiting and the number of applicants.

Before proceeding to the calculation of the correlation coefficient and our case study, it is important to describe some important aspects of this procedure. First, the correlation coefficient only measures a *linear* relationship. Any relationship that may be

curvilinear or otherwise non-linear will produce a correlation coefficient that is weak or non- significant. As a result, always draw a graph (scatterplot) of your data before calculating your correlation coefficient. The graph will provide you with some visual clues as to whether or not the relationship between your variables is linear.

All correlation coefficients range in value from +1.0 to -1.0 and measure two aspects of the relationship between the variables: direction and strength. The strength of the relationship measures how closely the data match a linear relationship. A correlation coefficient of Å 1.0 indicates that the data are perfectly linearly related, while a coefficient of 0 implies that no linear relationship exists.[1] The sign of the coefficient indicates the direction of the relationship. A positive coefficient indicates that as the value of one variable increases the value of the other variable also increases. On the other hand, a negative coefficient indicates that as the value of one variable increases the value of the other variable decreases, an inverse relationship.

A correlation coefficient of +1.0 indicates a perfect positive linear relationship, while a correlation coefficient of -1.0 indicates a perfect negative linear relationship. Rarely if ever will a researcher uncover a correlation coefficient of +1.0 or -1.0. Relationships are not that clearly defined in the social sciences. The combination of strength and direction best describes the relationships between variables. However, strength and direction are two independent qualities. A correlation of +.40 has equal strength but opposite direction to a coefficient of -.40. A sample of these relationships is best shown graphically in Figure 9. In some instances, the coding of the data may create a negative relationship. For example if high school class rank for applicants is correlated with SAT scores, a negative relationship may logically result. Normally, class rank is coded so that a 1 indicates first in the class. Since SAT is coded so that the higher the score the better, a negative relationship may be found between these two variables.

Pearson Correlation Coefficient

Basic Assumptions:

In this case study, the relationship between our two variables will be measured by calculating the Pearson Product-Moment Correlation Coefficient (PPMCC). The PPMCC is a parametric statistic. Therefore, in order to utilize this procedure both variables must be interval or ratio level of measurement, the distribution of scores should be essentially normal, and the sample size should be at least 30. All basic assumptions are met in our case study.

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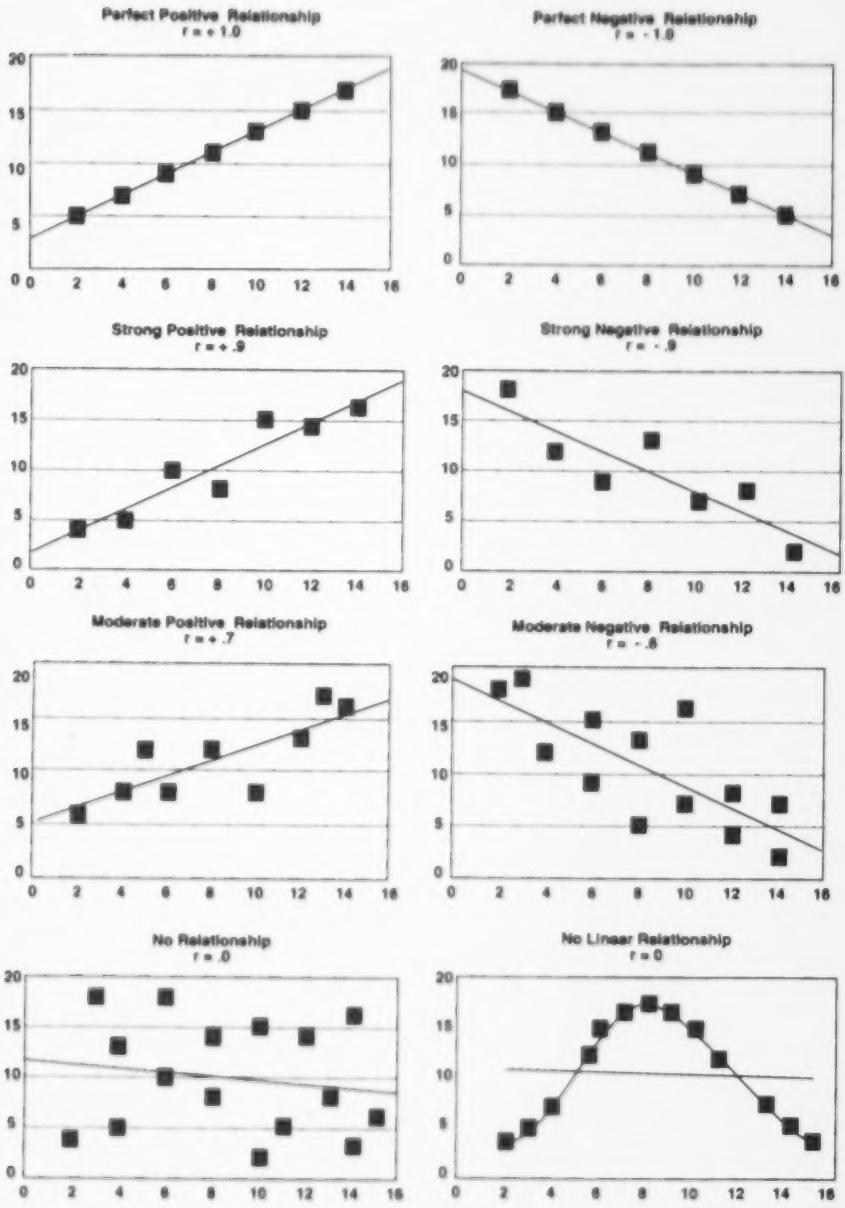
[1] Remember, a coefficient of 0 does not rule out the possibility of a curvilinear relationship.

Figure 9

Correlation Coefficients: Strength & Direction



Analysis of Data:

In this analysis, the two variables are high school grade point average (HSGPA)[2] and first-year GPA (LTDGPA). Again, the PPMCC was calculated to measure the strength and direction of the relationship between these two variables. The CORRELATIONS procedure from SPSS (Norusis, 1993) was used to calculate this statistic. For your reference, the formula for the PPMCC is listed below in Table 8 with the output from the SPSS procedure.

Table 8

Formula for

Pearson Product Moment Correlation Coefficient (PPMCC)

$$R = \frac{N\Sigma XY - (\Sigma X)(\Sigma Y)}{\sqrt{\left[N\Sigma X^2 - (\Sigma X)^2\right]\left[N\Sigma Y^2 - (\Sigma Y)^2\right]}}$$

SPSS Output from

Correlations Procedura (PPMCC)

```
- - Correlation Coefficients - -

          LTDGPA     HSGPA      VERB_SAT   MATH_SAT

LTDGPA    1.0000     .2342      .1656      .1355      strength & direction
          ( 635)     ( 621)     ( 615)     ( 615)     # of subjects
          p = .      p = .000   p = .000   p = .001   significance

HSGPA     .2342      1.0000     .1003      -.0993
          ( 621)     ( 621)     ( 566)     ( 566)
          p = .000   p = .      p = .895   p = .018

VERB_SAT  .1355      .1003      1.0000     .2549
          ( 615)     ( 566)     ( 615)     ( 615)
          p = .000   p = .895   p = .      p = .000

MATH_SAT  .1355      -.0993     .2549      1.0000
          ( 615)     ( 566)     ( 615)     ( 615)
          p = .001   p = .018   p = .000   p = .

     (Coefficient / (Cases) / Significance)

     * . * is printed if a coefficient cannot be computed
```

Reviewing the SPSS output provides a correlation matrix. The correlation coefficient between LTDGPA and high school grade point average (HSGPA) is the strongest reported ($r = .234$). While total unanimity does not exist with regard to

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[2] Depending on the variety of backgrounds of the entering first-year students, you may wish to convert raw high school grade point averages to standardized scores by calculating Z scores.

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interpreting correlation coefficients, some authors of basic statistics texts describe correlations of 0 to .29 as weak, .30 to .59 as moderate, and above .60 as strong (Levin & Fox, 1994). Thus, our correlation is weak. Also, the relationships between LTDGPA and SAT scores are weak (verbal, $r = .1656$; math, $r = .1355$). However, the question still remains, does a significant association exist between either high school grade point average or SAT scores and LTDGPA? In order to generalize about this relationship, a test of significance should be performed. The SPSS printout reports a significant positive linear relationship between all of these variables. This test of significance determines if the relationship is significantly different from 0. As a result, many moderate to weak correlations with a decent sample size ($n > 100$) will be statistically significant.[3]

In assessing the true strength of the relationship between the two variables, many researchers will calculate R^2, which is determined by squaring the correlation coefficient. R-squared is associated with regression analysis and determines the proportion of the total variation in the LTDGPA scores that can be explained by either high school grade point average or SAT scores. Also, $1 - R^2$ represents the proportion of this variance that is left unexplained or is due to other factors. In this analysis, 5.48% (.234 ★ .234) of the variability in the LTDGPA scores can be explained by the high school grade point average of first-year students. Therefore, while a significant relationship ($r = .234$, $p = .00$) does exist between the two variables, a large amount of the variance (94.5%) in LTDGPA remains unexplained or is due to other factors. As a result, the researcher should definitely proceed with caution in describing this relationship. SAT scores were not stronger predictors of first-year grade point average. The R^2 for verbal SAT is .027(2.7% explained) and for math .018 (1.8% explained).

Limitations to Correlational Analyses:

When interpreting correlation coefficients, several limitations should be considered, of which we have so far discussed two. First, the PPMCC only measures linear relationships; secondly, the test of significance for the correlation coefficient only determines whether or not the correlation coefficient is significantly different from 0. Beyond these two limitations, the researcher needs to be sure that he or she does not imply any cause and effect relationship between the two variables when discussing correlational findings. Remember, correlation measures the strength and direction of the relationship found between two variables. The researcher makes no attempt to manipulate or control these variables in any manner. Thus, no cause and effect conclusions may be drawn. Too many other unexplained or uncontrolled factors may be influencing this relationship, and you did not measure or control for these factors. Limit the wording of your interpretation to terms such as association, relationship, or link and avoid terms such as cause, effect, or difference. For example in this case study, an appropriate conclusion statement might

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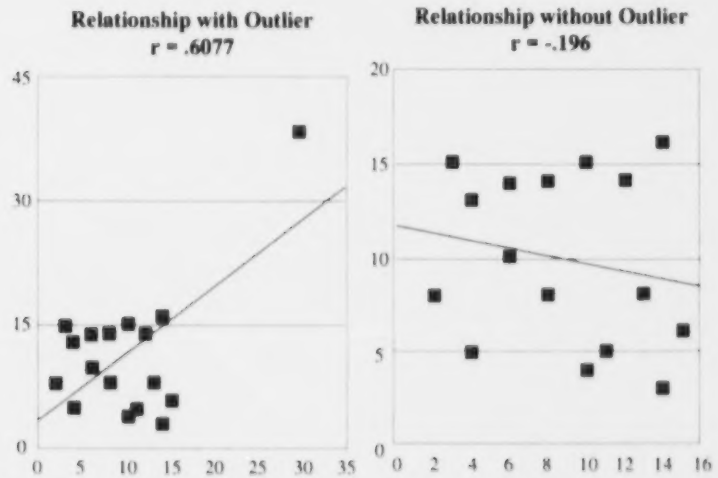
[3] For example, a correlation coefficient of greater than or equal to Å .196 with a sample size of 100 will be significant. In Institutional Research, larger sample sizes often exist, which does in some cases assist with statistical power.

read: a minimal positive association was found between high school GPA and first-year GPA.

Another factor that may hinder in the interpretation of correlation coefficients is the presence of an outlying score. An outlier is a score that falls outside of what would be considered the normal range of data values.[4] The presence of the outlying score may serve to positively or negatively inflate the value of the correlation coefficient. Often, this outlying score gives the relationship an added anchor point to assist in the fit to a linear relationship. A picture is worth a thousand words, so refer to Figure 10. In the first graph the value of the correlation coefficient is .608, and is found to be significant ($p = .01$). Yet, when the outlier is removed, the value of the coefficient is -.196 and is non-significant ($p = .47$). Remember, always graph your data; without the graph the outlier may go unnoticed.

Figure 10

Interpreting Correlation Coefficients: The Problem with Outliers



Similarly, having two groups that are known to be different on one or both of the variables can inflate the value of the correlation coefficient. Again, Figure 11 graphically displays this concept. The relationship between job-related stress and salary for Institutional Researchers is plotted. Notice the two distinct groupings of data points found on this graph. The group in the upper right hand corner are all males and in the lower left hand corner all females. The overall correlation is strong ($r = .913$) and

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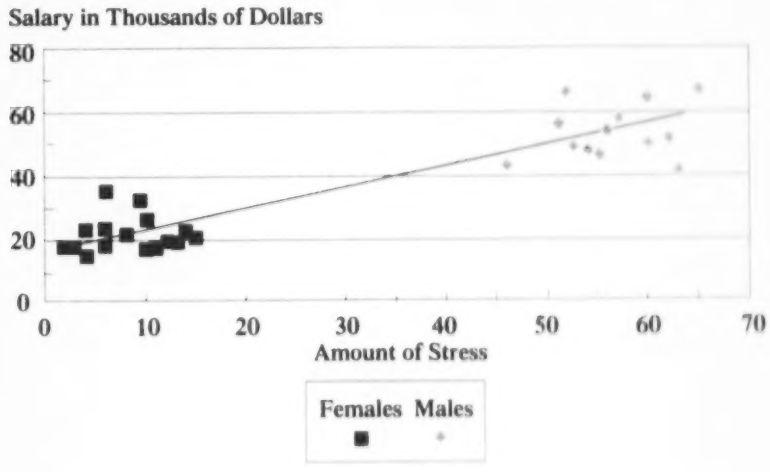
[4] Many researchers define an outlier as any score that falls above or below 2 standard deviations from the mean.

certainly the relationship is significant ($p = .00$). However, the linear relationship is being enhanced by the presence of the difference in means found between these two groups. In fact, when the correlation coefficients are calculated separately for males and females they drop drastically and are both non-significant (males, $r = .179$, $p = .49$; females $r = .033$, $p = .90$). Again, remember always to graph your data and be alert for this type of problem. If you suspect the presence of divergent groups on any one of your variables, do a test of mean difference prior to running your correlational analysis. When significant differences are found, calculate and report separate correlation coefficients for each group.

Figure 11

Interpreting Correlation Coefficients: The Problem with Divergent Groups



Other Statistical Procedures for Measuring Relationships

Non-parametric Correlations:

As mentioned previously, the PPMCC calculated in this case study is a parametric statistic. When the assumptions of a parametric statistic have been violated, several non-parametric correlational procedures exist. Within the bounds of this text, no attempt has been made to review all of these procedures; rather a brief example of one will be included. The nice aspect of all correlational procedures is that they generate a correlation coefficient, and the same universal characteristics of strength and direction apply to all coefficients.

Within the context of Institutional Research, the use of non-parametric procedures is often warranted because of the use of ordinal Likert scales. For example, a researcher may wish to know if a relationship exists between satisfaction with academic programs and the SAT scores of applicants. Due to the fact that satisfaction with the

academic program is rated on a 5-point Likert scale, the use of the PPMCC is not statistically appropriate; rather the Spearman Rank-Order Rho Correlation Coefficient would be an appropriate non-parametric equivalent. As the name implies, the Spearman Formula generates a separate ranking for each subject on both variables. The relationship between the order of the rankings for both variables is what is used to calculate the coefficient. The CORRELATIONS procedure from SPSS can also be used to calculate the Spearman Rank Order Rho correlation coefficient (SRORCC). For your reference, the formula for the SRORCC and the SPSS output for this procedure may be found in Table 9.

Table 9

Formula for

Spearman Rank Order Rho Correlation Coefficient (SRORCC)

$$R = 1 - \frac{6\,\Sigma d^2}{n(n^2 - 1)}$$

SPSS Output from

Correlations Procedure (SRORCC)

```
S P E A R M A N   C O R R E L A T I O N   C O E F F I C I E N T S

MATH_SAT          .3871
                  N( 615)
                  Sig .000

ACADPROG          .3441          .4433
                  N( 610)        N( 610)
                  Sig .000       Sig .000

                  VERB_SAT       MATH_SAT

(COEFFICIENT / (CASES)  /  2-TAILED SIGNIFICANCE)

" . " IS PRINTED IF A COEFFICIENT CANNOT BE COMPUTED
```

In reviewing the SPSS output, the SRORCC between verbal SAT and rating of academic program was found to be .334 and between math SAT and rating .443. Given the moderate strength of this coefficient and the fact that the correlation was statistically significant, the researcher would conclude that a significant positive linear relationship does exist between the ranking of satisfaction with academic program and SAT scores. In

simpler terms, as the applicant's ranking of his or her academic program increases, so does his or her SAT score. Overall good news for your institution.[5]

The Spearman correlation coefficient is a common non-parametric choice for evaluating relationships between ordinal variables or for any combination of ordinal with interval or ratio data. Other non-parametric choices include Goodman's or Kruskal's Gamma for ordinal data. The Phi coefficient measures the relationship between two nominal variables each with only two categories from a crosstabulation table (2 X 2). In addition, a Contingency Coefficient is used to measure the relationship between other larger crosstabulation tables.[6] The output of the SPSS procedure CROSSTABS will report the value of these coefficients.

Regression Analysis:

Correlation measures the linear relationship that exists between two variables. Once a correlation has been found between two variables the next logical question to ask is whether or not that relationship can be used to predict or explain one variable from the other. In correlation we have no true independent or dependent variable, because we are simply trying to measure the relationship between the two variables. However, in bi-variate regression one variable is defined as the dependent or criterion variable and the other variable is the independent or predictor variable. In this analysis, the knowledge of the independent variable (i.e., high school GPA) is used to predict or explain the dependent or criterion variable (i.e., first-year GPA). Besides being a logical progression from correlation, regression has a great deal of practical application for practitioners. In Institutional Research, regression analysis is most commonly applied to predict first-year GPA, from some combination of independent variables (e.g., SAT, HSGPA, admissions rating). After all, what better tool for admissions than to be able to accurately predict how a student will achieve academically?

As a brief example of regression, high school grade point average will be used to predict first-year GPA. In this model, first-year GPA is the criterion or dependent variable, and high school GPA is the predictor or independent variable. The

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[5] Remember, it is important not to imply any causal relationship between rating of program and SAT score. We did not manipulate either variable and thus have no knowledge of what other factors may be influencing or overlapping.

[6] Often beginning researchers believe that they want to measure the relationship between a nominal variable (e.g., gender) and some other dependent variable which is ordinal, interval, or ratio (e.g., LTDGPA, or SAT). However, this research design is not correlational, rather it is quasi-experimental. The researcher really wants to know if a difference exists between males and females with regard to the dependent variable. For more information on tests of differences refer to Chapter 3.

REGRESSION procedure from SPSS (Norusis, 1993) was used to calculate this statistic. The output from this procedure and a scatterplot displaying the relationship between these variables may be found in Table 10 and Figure 12.

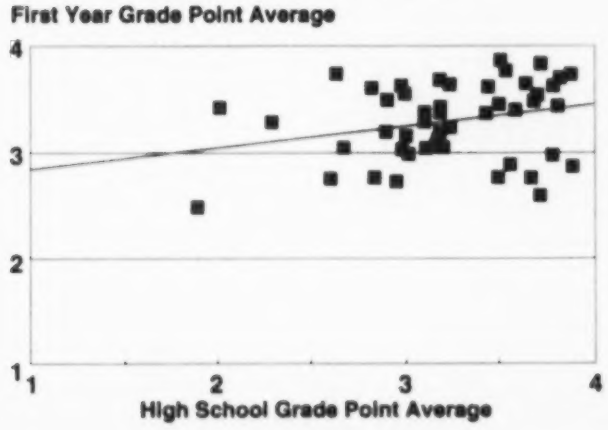
Table 10

SPSS Output from Regression Procedure

```
* * * * M U L T I P L E   R E G R E S S I O N * * * *

Equation Number 1  Dependent Variable . .  LTDGPA  Grade Point Average

Block  1.  Method:  Enter      HSGPA

Variable(s)  Entered on Step Number
  1 . .  HSGPA -- High School Grade Point Average

Multiple R           .23420
R Square             .05485
Adjusted R Square    .05322
Standard Error       .30872

Analysis of Variance
                  DF          Sum of Squares          Mean Square
Regression         1                3.19703                3.19703
Residual         578               55.08949                 .09531

F =   33.54330     Signif F  =  .0000

- - - - - - - - - - - - Variables in the Equation - - - - - - - - - - -

Variable             B         SE B         Beta          T       Sig T

HSGPA             .203590      .017980      .23420       5.792      .0000
(Constant)       2.634742      .053804                  32.152      .0000

End Block Number  1  All requested variables entered.
```

Figure 12

Scatterplot with Regression Line



The crux of the regression analysis centers on fitting a straight or linear line through the points on the scatterplot. The line is determined so that the distance between each and every point (i.e., X, Y coordinates) and this line is the smallest possible distance. The formula for a straight line is $Y' = a + bX$. Two elements of this formula are the constant or y-intercept (a) and the slope or regression coefficient (b). The constant or y-intercept represents the value of Y when X is 0. In other words, the slope is the direction and intensity of the line and the y-intercept can be thought of as the starting point of the line. In this analysis, the constant represents an average of first-year GPA for all students when high school grade point average is 0. However, since a 0 for high school GPA is not possible, the interpretation of this value is very limited at best. The slope represents the amount that the criterion variable increases or decreases in response to a one unit change in the predictor variable. In this analysis, the slope represents the average change in first-year GPA for a one unit change in high school GPA.

The beauty of regression analysis is that with the creation of the regression line, the researcher now can make a predicted score for any value of the predictor variable found within the range of the original data values. Predicted scores (Y') may be found by inserting the value of predictor variable (X) into the regression equation and solving for Y'. In this analysis, the regression equation is $Y' = 2.63 + .204X$. All predicted scores are found on the regression line, which is plotted on the scatterplot (Figure 12).

Once the predicted score has been created, the next logical question is how good is your prediction? To answer this question, researchers may refer to two elements of the SPSS printout, the significance level of the slope (b) and the R^2 value. The significance level of the slope determines whether the independent variable is a significant predictor of the criterion measure. In this analysis, the significance level is .00, so high school GPA is able to significantly contribute to the prediction of first-year GPA. As described earlier, R^2 represents the total amount of dependent score variance that can be explained by the independent or predictor variables. In this analysis, 5.4 percent of the first-year GPA can be explained by the high school GPA of first-year students. So while, high school GPA is a significant predictor of first-year GPA, 95.4 percent of the first-year GPA is unexplained or due to other factors. Would you be willing to bet on the accuracy of this prediction or do you feel that the model has limitations? The model is very limited.

Several forms of regression analysis exist, the simplest of which is bivariate regression. As described above, bivariate regression refers to the analysis in which one predictor variable is used to explain one criterion variable. While this model is the easiest to conceptualize, the model is severely limited in that not often is any criterion variable able to be fully explained by one predictor variable. In this case study, first-year GPA could not fully be explained by knowing the high school GPA of entering students. Multiple regression encompasses all designs in which multiple predictor variables are used to explain one dependent or criterion measure. Both of the above mentioned procedures require that all variables used in the model be interval or ratio in measure.[7]

Logistic regression is another form of regression for designs in which a nominal dependent variable is predicted from some combination of ordinal, interval, or ratio independent variables. In Institutional Research, Logistic Regression has been commonly used to predict enrollment status (enrolled vs. non-enrolled) from some combination of predictor variables taken from an applicant data base (e.g., SAT, HSGPA, and ratings of various aspects of your institution).

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[7] However, some coding procedures do exist for using nominal variables in regression analysis. The most common of these is dummy coding for a nominal variable with two levels or categories. While further discussion of these procedures is beyond the scope of this text, refer to Pedhauzer & Schmelkin (1991) for elaboration of these procedures.

Chapter Four

Chi-Square: Differences in the Frequency of Enrolling and Non-Enrolling Students by the Quantity of Aid Offered

Case Study:

With the rising cost of a college education, the majority of individuals applying to institutions of higher education are also applying for financial aid. The rising cost of education and the failure of government aid programs to keep pace with these increases have made it more and more difficult for colleges and universities to meet the very real need of applicants for aid. In recruiting and enrolling quality applicants, financial aid is a crucial component.

This case involves a small private college with professional and pre-professional programs. The Vice-President for Enrollment Management has asked you to examine the percentage of need that is being met for a set of admitted students and how that impacts their enrollment status. The institution has a goal of meeting at least 60 percent of the demonstrated need of students. To date, the institution has been unable to reach this goal.

While the overall issues of financial aid and the associated budgetary impacts are quite complex, the task requested by the Vice-President is more limited. The focus of this case study is to examine the 300 applicants who are deemed the most qualified candidates by the admissions office, and to determine whether the frequency of enrollment is higher for those students whose package met or exceeded the college's goal of awarding 60 percent of need. From the financial aid office you must obtain the level of need met for each of these accepted applicants and assign it into one of two categories: at or above the 60 percent goal, or less than the 60 percent goal. In addition, from your administrative files you must identify enrollment status (i.e., enrolled versus non-enrolled). This case study will be used to illustrate the application of the chi-square test statistic. More specifically, the statistic is a 2 X 2 chi-square. Two choices exist for enrollment (i.e., enrolled or not enrolled) and two choices for aid (i.e., 60% of need is met or not met). Example Box 6 illustrates this design.

Example Box 6

		Enrollment Status	
		Enrolled	Not Enrolled
60 % of Need	Met		
	Not Met		

Background

The chi-square test statistic compares the frequency of occurrence to one or more nominal or ordinal variables. Two commonly used forms of the chi-square test statistic are the one-way and the two-way chi-square. In a one-way chi-square, the researcher is attempting to determine whether the frequencies observed in the variable differ significantly from some previously anticipated distribution of responses, usually an equal distribution. In a two-way chi-square, the researcher is comparing the distribution of one variable (i.e., the dependent variable) across the categories of the other variable (i.e., the independent variable).

Before proceeding to the calculation of the two-way chi-square and our case study, describing some characteristics of this test statistic is important. The focal point of the chi-square analysis is the comparison of the frequency of occurrence of a given characteristic(s) or response(s). Some researchers refer to the two-way procedure as a test of independence. In other words, do the responses observed for the independent variable provide any knowledge of the dependent variable? Variables are said to be independent when knowing the value of one variable will not help to predict the value of the other. Variables are said to be dependent or associated when knowing the value of one helps you to predict the other.

Two important terms in chi-square are observed and expected frequencies. Observed frequencies (fo) are the actual results 'observed' in our data. They are the number of subjects who were observed within each of the categories or cells. In contrast expected frequencies (fe) are based on the theoretical number of people who would fall into each category assuming some particular hypothesis. Most researchers assume the null hypothesis that an equal number of people should fall into each category or that no differences are expected in the frequencies. The observed frequencies then are the actual data and the expected frequencies are based on a theoretical model or independence between the variables. Since the calculation of the chi-square centers on the analysis of the differences between observed and expected frequencies, when the difference between expected and observed frequencies is large enough, the null hypothesis is rejected. Then the conclusion can be made that the two variables are dependent or that a true population difference exists.[1]

Two-way Chi-Square

Basic Assumptions:

Chi-square is a non-parametric statistic. As a result, chi-square can be designed to be used on all levels of data. The procedure requires that data be grouped into either nominal or ordinal categories. Therefore, interval or ratio data must be recoded in order to be analyzed through this statistic.

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[1] Chi-square can be used as a test of association between two or more nominal or higher variables. Within the context of this text, chi-square is being explored as a non-parametric test of differences between the frequency of response to two or more nominal or ordinal variables.

A second statistical assumption of the two-way chi-square is that the *expected frequencies* should not be too small. Authors of most basic statistics texts suggest that the expected frequency in any one cell or category be not less than 5 (Levin & Fox, 1994, Triola, 1995). For 2 X 2 chi-square tests, a correction formula for small expected frequencies, Yates' Correction, exists and is provided on the SPSS output. However for other designs, no global correction factor exists. When the number of cells with expected frequencies less than 5 is large,[2] merging categories together wherever logical or plausible is highly recommended.

Analysis of Data:

In this analysis, the two variables are percentage of need met ($\geq 60\%$, or $< 60\%$) and enrollment status (enrolled, or non-enrolled). The 2 X 2 chi-square is calculated to determine whether a difference exists in the frequency of enrolled and non-enrolled applicants between the levels of need met. The CROSSTABS procedure from SPSS (Norusis, 1993) was used to calculate this statistic. The formula for the chi-square (χ^2) and the output from the SPSS procedure are presented in Table 11.

At the heart of the analysis of the χ^2 is the crosstabulation or contingency table. A contingency table is a distribution in which the frequencies correspond to combinations of the values of two variables. The row variable defines the dependent variable for the χ^2 and the column variable the independent variable. Since we wish to determine whether enrollment is dependent upon financial aid, percentage of financial aid met is the independent variable and enrollment status is the dependent. Cells are found at the intersection of each row and column. For example, in our crosstabulation table in Table 11 the frequency for the first cell is 113 and represents the number of enrolled applicants with ≥ 60 percent of need met who enrolled. From within the SPSS procedure CROSSTABS, the user can customize the output provided in each cell. The most commonly requested and helpful values are observed frequencies and column percent. Again, observed frequencies represent the actual responses for each category or cell. The column percentages are obtained by dividing the observed frequency by the number of subjects or cases in that column and then multiplying by 100. The observed frequency for this first cell is 113 with a corresponding column percentage of 59.2.

Other cell information that can be requested includes: row percent, total percent, expected frequency, and residuals. However, it has been our experience that keeping the amount of information requested in the cells to a minimum prevents misinterpretation. Row percentages provide the distribution of the column variable for each value of the row variable. In this analysis, these percentages represent the distribution of percentage of need met for each level of enrollment status. Given that percentage of need is our independent variable and enrollment status our dependent variable, these percentages are not necessarily meaningful, which is why column percentages were requested. Total percent represents the percentage results for the two variables jointly and is

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[2] Large is normally defined as 20 percent or more of all cells.

Table 11

Formula for Chi-Square Test Statistic (χ^2)

$$\chi^2 = \sum \frac{(fo-fe)^2}{fe}$$

SPSS Output from CROSSTABS Procedure

ENROLL Enrollment Status by NEED Amount of Need Met

NEED Page 1 of 1

ENROLL	Count / Col Pct	=> 60%	< 60%	Row Total
		1.00	2.00	
1.00 enrolled		113	34	147
		59.2	31.2	49.0
2.00 Non-enrolled		78	75	153
		40.8	68.8	51.0
	Column Total	191	109	300
		63.7	36.3	100.0

Chi-Square	Value	DF	Significant
Pearson	21.72432	1	.00000
Continuity Forrection	20.61950	1	.00001

Minimum Expected Frequency - 53.410

Number of Missing Observations: 0

calculated by dividing the observed frequency by the total number of subjects or cases in the sample and then multiplying by 100. Total percentages can be ambiguous and misleading because they do not provide any balance based on the number of individuals in either the row or the column.

Expected frequencies represent the null hypothesis and describe the theoretical number of individuals who would be found in each cell if no association existed between the two variables. The formula for expected frequency is:

f_e = (number in the row * number in the column) / total N

Residual values are crucial to the calculation of the chi-square. Residuals measure the differences between what was observed and what is expected. Several forms of residual values can be calculated: unstandardized, standardized, and adjusted standardized. However, the unstandardized residual values are the most common and easiest to understand. Unstandardized residuals represent the difference between observed and expected frequencies (fo - fe values). The sum of the unstandardized residuals will always equal zero. Since both observed and expected frequencies account for all subjects, the

sum of the difference between these two values must always balance each other.

The next step in calculating the x^2 is to square the residual values. As we saw in Chapter 1 when we calculated variance, the procedure for eliminating the negative sign of a value is to square the number. Next, the x^2 formula calls for the researcher to divide the squared residual $[(fo - fe)^2]$ by expected frequency (f_e). The final x^2 value is found by summing each of these values across all cells. The SPSS output reported in Table 11 indicates that this x^2 value, labeled Pearson, is 21.52. That is Pearson as in Karl Pearson of Pearson Product-Moment Correlation Coefficient fame who also developed this chi-square formula. Table 12 illustrates the above mentioned calculations for this data.

Table 12

Calculations for Two-Way Chi-Square

Observed Frequency

	=> 60%	<60%	Total
Enrolled	113	34	147
Non-Enrolled	78	75	153
Total	191	109	300

Expected Frequency

fe=(# in row*# in column) / Total N

	=> 60%	<60%
Enrolled	93.59	53.41
Non-Enrolled	97.41	55.59

Calculations of Two-Way Chi-Square

Cells	fo	fe	fo-fe	(fo-fe)2	(fo-fe)2/fe
=> 60% Enrolled	113	93.59	19.41	376.7481	3.8214
=> 60% Non-Enrolled	78	97.41	-19.41	376.7481	3.8677
<60% Enrolled	34	53.41	-19.41	376.7481	7.0539
<60% Non-Enrolled	75	55.59	19.41	376.7481	6.7773

E(fo-fe) 2fe = 21.5203

A x^2 value of zero indicates that observed frequencies are identical to expected values. Thus, the larger the x^2, the larger the difference between observed and expected frequencies. However, the question still remains: Does a significant difference in the frequency of enrollment status exist between those applicants who had ≥ 60 percent of need met and those who did not? Of course, in order to generalize about this difference a test of significance must be performed. According to the SPSS output, our chi-square value is significant ($p = .00$). Thus, percentage of need met and enrollment status are associated. However, we still need to know: Which level of percentage of need is more likely to have a higher level of enrolled students?

In order to further analyze the differences found in this x^2, the researcher has two options. Option one is to calculate separate one-way chi square values for each column of the crosstabulation table;[1] reporting the finding and statistical significance separately for each level of the dependent variable. A second option would involve reviewing the table and identifying differences in column percentages above a certain value as significant.[4] Either one of these column analyses should be done to better interpret the overall significant ($p < .05$) chi square. Little value is found in saying that a significant difference exists in the frequency of enrolled and non-enrolled applicants between the levels of percentage of need met, without saying where the differences were. A more specific statement is necessary. However, option one is by far the more preferable method to determine statistically where these significant differences exist. Option two does not contain any test of statistical significance. In some instances, where the trends are so obviously seen in the column percentages, this additional step may be nothing more than tedious paperwork.

In completing this analysis, the one-way analyses were run separately for each level of need: ≥ 60%, < 60%. The results may be found in Table 13. Significantly more students who had 60 percent or more of their need met enrolled at the College. Conversely, significantly more students who had less than 60 percent of their need met did not enroll.

Table 13
SPSS Output from NPAR Tests
Separate One-Way for Each Level of Need

NEED: 1.00 => 60%

- - - - - - Chi-Square Test

ENROLL Enrollment Status

	Category	Cases Observed	Expected	Residual
enrolled	1.00	113	95.50	17.50
non-enrolled	2.00	78	95.50	-17.50
	Total	191		

Chi-Square	D.F.	Significance
6.4136	1	.0113

NEED: 2.00 < 60%

- - - - - - Chi-Square Test

ENROLL Enrollment Status

	Category	Cases Observed	Expected	Residual
enrolled	1.00	34	54.50	-20.50
non-enrolled	2.00	78	54.50	20.50
	Total	191		

Chi-Square	D.F.	Significance
15.4220	1	.0001

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[1] The easiest way to run these separate one-way chi-squares is to use the SPLIT FILES procedure in SPSS (Norusis, 1993). The split files command will run the NPAR TESTS procedure repeatedly for each level of the dependent variable.

[4] Some researchers define this value as anywhere from 5 to 10 percent; however, any value picked is arbitrary.

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Limitations in Chi-Square Analyses:

The chi-square statistical procedure is one of the statistical procedures most commonly used by Institutional Researchers. Many reasons exist for the widespread use of chi-square in Institutional Research. The majority of the variables analyzed by Institutional Researchers are nominal or ordinal in nature. Thus, many of our research questions focus on the frequency with which certain events occur. Additionally, chi-square is a basic statistical procedure that is familiar to most Institutional Researchers. While the applications for chi-square in Institutional Research are many, some limitations also exist.

For a chi-square analysis to be valid, the categories of the variables must be discrete and mutually exclusive (i.e., nominal or ordinal level of measurement). Often, Institutional Researchers will take a variable that is continuous in nature and collapse the data into ordinal categories. In this case study, the variable percentage of need met is a ratio variable, which was collapsed into nominal categories (i.e., ≥ 60%, and < 60 percent). From our case study, Table 14 shows the frequency distribution of the percentage of need variable both before and after recoding. By recoding need percentage, the researcher has lost valuable information. For example, do other percentage break downs make a difference in enrollment status? What is the mean difference in the percentage of need met between enrolled and non-enrolled applicants? Chi-square is not the appropriate test statistic to answer the latter of these two questions; a t-test is statistically appropriate.

Table 14

SPSS Output from FREQUENCY Procedure

Before Recode

PERNEED Actual Percentage of Need Met

Variable	Value	Frequency	Percent	Valid Percent	Cum Percent
	15.00	1	1.0	1.0	1.0
	20.00	10	9.0	9.0	9.0
	25.00	10	9.0	9.0	17.0
	26.00	5	4.0	4.0	21.0
	27.00	4	3.0	3.0	24.0
	28.00	3	2.0	2.0	26.0
	29.00	4	3.0	3.0	29.0
	30.00	1	1.0	1.0	30.0
	31.00	1	1.0	1.0	31.0
	32.00	1	1.0	1.0	32.0
	33.00	2	2.0	2.0	34.0
	34.00	1	1.0	1.0	35.0
	35.00	4	3.0	3.0	38.0
	36.00	1	1.0	1.0	39.0
	37.00	1	1.0	1.0	40.0
	38.00	1	1.0	1.0	41.0
	39.00	1	1.0	1.0	42.0
	40.00	10	7.0	7.0	49.0
	41.00	2	2.0	2.0	51.0
	42.00	1	1.0	1.0	52.0
	43.00	1	1.0	1.0	53.0
	44.00	1	1.0	1.0	54.0
	45.00	2	2.0	2.0	56.0
	46.00	1	1.0	1.0	57.0
	47.00	1	1.0	1.0	58.0
	48.00	1	1.0	1.0	59.0
	49.00	1	1.0	1.0	60.0
	50.00	4	3.0	3.0	63.0
	51.00	2	2.0	2.0	65.0
	52.00	1	1.0	1.0	66.0
	53.00	1	1.0	1.0	67.0
	54.00	1	1.0	1.0	68.0
	55.00	2	2.0	2.0	70.0
	56.00	1	1.0	1.0	71.0
	57.00	1	1.0	1.0	72.0
	58.00	1	1.0	1.0	73.0
	59.00	1	1.0	1.0	74.0
	60.00	4	3.0	3.0	77.0
	61.00	18	14.0	14.0	91.0
	62.00	16	12.0	12.0	83.0
	63.00	1	1.0	1.0	84.0
	64.00	2	2.0	2.0	86.0
	65.00	2	2.0	2.0	88.0
	70.00	2	2.0	2.0	90.0
	71.00	1	1.0	1.0	91.0
	72.00	1	1.0	1.0	92.0
	73.00	2	2.0	2.0	94.0
	74.00	1	1.0	1.0	95.0
	75.00	1	1.0	1.0	96.0
	77.00	1	1.0	1.0	97.0
	78.00	1	1.0	1.0	98.0
	79.00	1	1.0	1.0	99.0
	80.00	1	1.0	1.0	100.0
	Total	100	100.0	100.0	

Valid cases 100 Missing cases 0

After Recode

NEED Percentage of Need Met

Value Label	Value	Frequency	Percent	Valid Percent	Cum Percent
>= 60%	1.00	141	83.7	83.7	83.7
< 60%	2.00	159	16.3	16.3	100.0
	Total	100	100.0	100.0	

Valid cases 100 Missing cases 0

As mentioned earlier, a basic assumption of the chi-square test statistic is that the minimum expected frequency for any one cell should not be less than 5. Often when many cells with low expected frequencies are present, the researcher will merge or combine similar categories to create cells with larger expected frequencies. For example, when analyzing differences in levels of satisfaction between males and females from a Likert scale, the researcher may combine the categories of 'very dissatisfied' with 'somewhat dissatisfied' and 'very satisfied' with 'somewhat satisfied' to meet this basic assumption of the chi-square. Again, the major problem with this solution is the loss of information; the differences in the extremes are no longer distinguishable. Often the researcher is better off performing a non-parametric test for differences between groups, such as the Mann Whitney U test, to analyze the differences in Likert scale responses.

Other Statistical Procedures

One-way Chi-square:

Often Institutional Researchers look at a frequency distribution and wonder if a pattern exists in the responses to the item or question. The one-way chi-square is a test statistic that allows the researcher to determine whether the frequencies observed in the variable differ significantly from an anticipated distribution of responses. In this case study, the Institutional Researcher may wish to explore further the amount of need that is being met for all applicants to attempt to determine where the College stands in regards to the goal of meeting at least 60 percent of documented need.

To further explore this topic, the researcher goes back to the financial aid file and retrieves percent of documented need met for all 460 applicants. To facilitate the process the researcher recodes the actual percentage of need into five categories: 0 to 19%, 20 to 39%, 40 to 59%, 60 to 79% and 80 to 100%. After recoding the data, the FREQUENCY Procedure from SPSS (Norusis, 1993) is run to create a frequency distribution, followed by the NPAR TESTS procedure to calculate the one-way chi-square test statistic. The output from these two procedures may be found in Table 15.

From the SPSS procedure NPAR TESTS, notice that the calculation of the one-way chi-square follows the same procedures and formulas as presented for the two-way chi-square. The procedures are simplified by the fact that the expected frequencies represent an equal distribution of respondents in each of the categories. For our analysis, the expected frequency for each category is 92 (i.e., 460 divided by 5), the calculated chi-square value is 5.57, and the corresponding significance of the chi-square value is .23. Thus, no significant difference exists in the frequency of applicants receiving the various levels of percentage of documented need. Unfortunately for the institution, the data do not support the claim that the College is making progress toward meeting a minimum of 60 percent of the documented need of the applicant. In fact, students were just as likely to get less than 60 percent of need met as they were to get 60 percent or more. In order to support this claim, a significant difference would exist with significantly more students falling in the higher categories of percentage of need.

Table 15

SPSS Output from FREQUENCY Procedure

NEED Amount of Need Met

Value Label	Value	Frequency	Percent	Valid Percent	Cum Percent
0 to 19%	1.00	85	18.5	18.5	18.5
20 to 39%	2.00	95	20.7	20.7	39.1
40 to 59%	3.00	89	19.3	19.3	58.5
60 to 79%	4.00	110	23.9	23.9	82.4
80 to 100%	5.00	81	17.6	17.6	100.0
Total		460	100.0	100.0	

Valid Cases 460 Missing cases 0

SPSS Output from NPAR Tests

- - - - - - - - Chi-Square Test

NEED Amount of Need Met

Category		Cases Observed	Expected	Residual
0 to 19%	1.00	85	92.00	-7.00
20 to 39%	2.00	95	92.00	3.00
40 to 59%	3.00	89	92.00	-3.00
60 to 79%	4.00	110	92.00	18.00
80 to 100%	5.00	81	92.00	-11.00
Total		460		

Chi-Square	D.F.	Significance
5.5652	4	.2341

Chi-Square Automatic Interaction Detection (CHAID)

CHAID is a more advanced statistical procedure that has potential applications in Institutional Research. The statistical algorithm for CHAID was based upon the Automatic Interaction Detection (AID) procedure developed in the 1960's. AID was linked in theory and application to "Tree Analysis" which was commonly used in segmentation analysis and marketing research. The overall goal of all of these procedures is the discovery and specification of population groups (i.e., segments) that differ in their

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probability of a given event (i.e., the dependent variable). For example, in Institutional Research we are very interested in discovering whether certain segments or subgroups of our applicant pool have a higher probability of enrolling at our institution or whether any segments or subgroups of our student population are at a greater risk of withdrawing. Thus, the overall goal of CHAID and other segmentation modeling procedures is to divide the population into mutually exclusive and exhaustive subgroups (i.e., the segments) which differ with respect to the dependent variable (e.g., enrolling or not enrolling), and to identify those segments that are "best" from a marketing perspective, so that they can be targeted.

At first glance, CHAID appears to be most commonly related to the chi-square test statistic; however, CHAID procedures are squarely grounded in regression theory. CHAID begins by identifying the "best predictor" of the dependent variable (e.g., enrolling or withdrawing) and splits the population into distinct groups based upon the categories of the "best predictor." Once a variable has been defined as the "best predictor" variable, CHAID will create a two-way crosstabulation of this variable with the dependent variable. At this point, CHAID will attempt to create optimally merged categories of this predictor variable using a form of chi-square analysis. CHAID then performs these operations in an iterative process until all subgroups have been analyzed or contain too few observations.

Please be reminded that the CHAID procedure is an advanced and complex statistical procedure with a variety of different options. A complete explanation of this procedure would be beyond the scope of this text. For a more complete description of the CHAID procedures, refer to Madgison (1992).

Chapter Five

Selecting the Appropriate Statistic

One of the most puzzling dilemmas for novice statisticians is the decision concerning which statistical procedure is appropriate for the data at hand. It has been our experience that many people are quickly able to carry out a procedure to which they have been specifically directed. Thus, identifying the appropriate procedure is much more difficult than actually carrying out the analysis. In order to accelerate the learning curve, several variations of a statistical decision tree have been developed (Emory & Cooper, 1991; Kervin, 1992; Zikmund, 1992). Each model has its own strengths and weaknesses. The statistical decision tree described in this chapter was initially developed by Dr. Robert Lussier of Springfield College and was later revised in conjunction with Mary Ann Coughlin. A copy of the tree is found in Figure 13. The following text describes the nomenclature used in the tree and walks the reader through the decision tree using the case studies that were cited in the previous chapters.

The design tree shown in Figure 13 is meant to be a tool to help you answer the difficult question: What statistical procedure is appropriate for this design? Computer software, such as SPSS (Norusis, 1993), has made performing complex statistical procedures as easy as pointing and clicking. However, using these tools is the easy part; understanding and appropriately interpreting the analysis is harder. No tool should replace a solid understanding of the statistical procedure you are about to use. A very real danger exists in blindly performing advanced statistical procedures without an understanding of the underpinnings of these procedures. Several good references exist for advanced statistical procedures (Norman & Streiner, 1986; Norusis, 1993; Pedhauzer & Schmelkin, 1991). However, the tree presents a solid outline for identifying the appropriate statistical procedure for your analysis.

Using the Design Tree

The design tree was developed following the model of a flow chart. The user starts on the far lefthand side of the first page and answers a series of questions found in the columns of the chart. The answers to each of the questions lead the user to the last column which lists the correct statistical procedure based on the design. The questions are designed to determine key pieces of information about the research design that will determine which statistical procedure is appropriate.

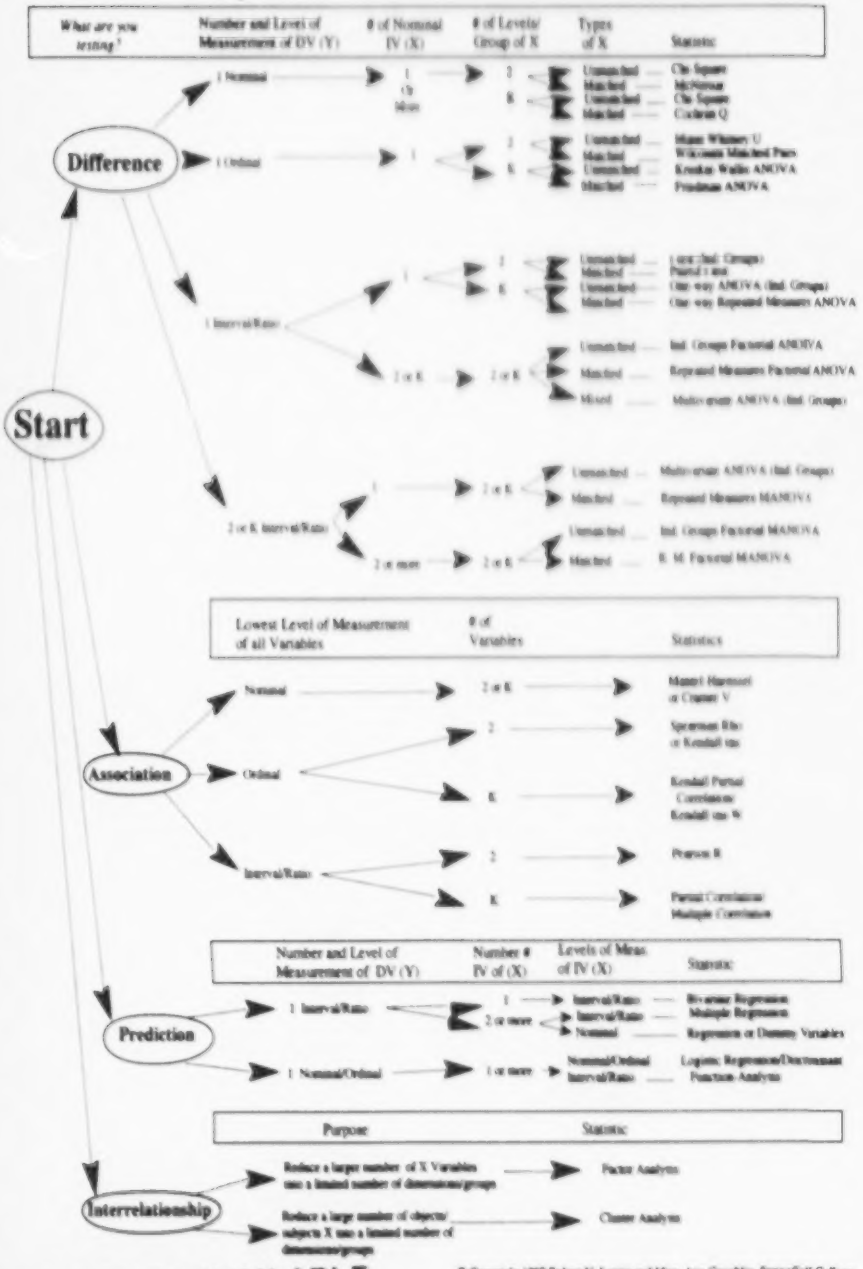
Before proceeding to describe the questions, learning some key abbreviations is important. First as you would expect, **DV** or **Y**[1] is synonymous with the dependent variable, and **IV** or **X** with the independent variable. However, the fact that **k** stands for 3 or more is

---

[1] For your convenience, throughout the remainder of the chapter terms and values are bolded when they appear on the design tree.

Figure 13

Selecting Appropriate Statistical Techniques: A Design Tree



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less obvious. So that "independent groups" does not get confused with "independent variable," the term **unmatched** is a synonym for independent groups, while **matched** is synonymous with repeated measures. For a review of some of these basic terms, refer to Chapter 1 for a discussion of independent and dependent variables, and Chapter 2 for independent groups and repeated measures.

The first question asks ***"What are you testing?"*** and has four possible response options: **difference**, **association**, **prediction**, and **interrelationship**. A test of **differences** is designed to examine whether differences of a significant magnitude exist between the levels of one or more independent variables with regard to some dependent measure(s). Within the scope of this text, tests of differences were discussed in Chapter 2 and Chapter 4. In Chapter 2, differences in faculty salaries between the genders and divisional status were explored. In Chapter 4, differences in frequencies were explored between enrolling and non-enrolling students across the levels of financial aid received. Tests of **association** measure the strength and direction of relationships between two or more variables. Tests of association were discussed in Chapter 3, when the relationship between high school grade point average and first-year grade point average was explored. Tests of **prediction** are used to assess the accuracy of predictions about the dependent variable based upon the knowledge of the independent variable. A brief introduction to tests of prediction was provided in Chapter 3, when the ability of high school grade point average to predict first-year grade point average was explored with regression analysis. Finally, tests of **interrelationships** are used to reduce or group a large number of associated variables, subjects, or objects into smaller groupings. The two statistical procedures described in this section of the design tree are factor analysis and cluster analysis. These procedures are included in the design tree to make the tree as complete as possible, but are beyond the scope of this introductory text.

The remaining questions on the design tree all have to do with important issues regarding the assumptions of the statistical procedures and how these assumptions relate to your research design. The questions vary slightly with the purpose of your research (i.e., ***what you are testing***: **difference**, **association**, **prediction** or **interrelationship**). Most of the questions center around the number and level of measurement of your independent and dependent variables, as well as the type of independent variable. For a review of the levels of measurement variables refer to Chapter 1; for a discussion of the type of independent variable (independent groups, repeated measures,[2] or mixed) refer to Chapter 2.

Examples of the Design Tree:

To provide some brief examples of the design tree, each case study will be re-examined. The first case study, provided in Chapter 1, sought to determine whether differences existed between the salary of male and female assistant professors. Given that our purpose is to determine whether differences exist, the answer to the first question on

---

[2] Remember, **unmatched** is synonymous with independent groups and **matched** is synonymous with repeated measures.

the design tree - what are you testing - is **difference**. So from the **Start** circle, follow the arrow up to **difference**. The next column asks the question, what is the number and level of measurement of the dependent variable? The dependent variable in this case study is salary, so one dependent variable exists and is measured at the ratio level. Follow the arrow down to **1 Interval/Ratio**. The next column asks how many independent variables are in this design. The answer is **1** (gender), so follow the arrow straight across to **1**. The next column asks how many levels or groups exist within the independent variable? Since gender has two levels or groups (i.e., male and female), follow the arrow straight across to **2**. The final question asks what type of independent variable is gender. Since gender is an independent groups variable (i.e., individuals are either male or female), follow the arrow straight across to **unmatched**.[2] In the last column across from **unmatched**, the appropriate statistical procedure is listed, **independent groups t-test**.

Our second case study in Chapter 3 explored the relationship between high school grade point average and first-year grade point average. Given that our purpose is to measure relationships, the answer to the first question on the design tree, **what are you testing**, is **association**. So from the **Start** circle, follow the arrow down to the second page to **association**. The next column asks what is the lowest level of measurement of all of the variables. Since high school grade point average and first-year grade point average are both interval level of measurement, follow the arrow down to **Interval/Ratio**. The next question asks how many variables are being analyzed. In this design, the relationship is between two variables, high school grade point average and first-year grade point average, so follow the arrow straight across to **2**. The last column across from **2** lists the appropriate statistical procedure, **Pearson correlation coefficient (R)**.

In Chapter 4, the case study attempted to determine whether significant differences existed between the enrollment pattern of applicants who were awarded grants that matched or exceeded 60 percent of their documented need and those whose award did not meet 60 percent of their need. Given that our purpose is to determine if differences exist, the answer to the first question on the design tree, **what are you testing**, is **difference**. So from the **Start** circle, follow the arrow up to **difference**. The next column asks what the number and level of measurement of the dependent variable is. The dependent variable in this case study is enrollment status, so one dependent variable exists and is at the nominal level of measurement. Follow the arrow up to **1 nominal**. The next column asks how many independent variables are in this design. The answer is 1 (amount of need met), so follow the arrow straight across to **1 or more**. The next column asks how many levels or groups exist within the independent variable. Since amount of need met has two levels or groups (i.e., $\geq 60\%$ and $< 60\%$), follow the arrow straight across to **2**. The final question asks what type of independent variable is amount of need met. Since amount of need is an independent groups variable, follow the arrow straight across to **unmatched**.[2] In the last column across from unmatched, the appropriate statistical procedure is listed, **chi-square**.

Appendix A

SPSS Commands

The following is a list of SPSS menu selections that were run to perform the analyses discussed throughout this text. To replicate any of the output, follow the basic set of menu selections.

For FREQUENCIES:

```
Statistics
      Summarize
            Frequencies
            Enter all of your variables
                  Statistics
                        Quartiles
                        Mean
                        Median
                        Mode
                        Sum
        Standard Deviation     Minimum     Skewness
        Variance               Maximum     Kurtosis
      Continue
      OK
```

For Independent Groups t-test:

```
Statistics
      Compare Means
            Independent Samples t Test
               Test Variable = Dependent variable
               Grouping Variable = independent variable
                     Define Groups
                              Group 1 = 1
                              Group 2 = 2
   Continue
   OK
```

For One-way ANOVA:

```
Statistics
   Compare Means
      One-Way ANOVA
      Test Score -> Dependent Variable Box
      Ind. Var. -> Factor Box
   Define Range
      Minimum lowest
      Maximum highest
   Continue
   Post Hoc
      x Least Significant Difference
      x Student Newman-Keuls
      x Tukey HSD
      x Scheffe

   Continue
   Options
      x Descriptives
      x Homogeneity of Variance
   Continue
                        OK
```

For Correlation (Either Pearson or Spearman):

```
Statistics
   Correlate
      Bivariate
         Move TWO VARIABLES into the Variable Box

Check either Pearson or Spearman and leave other two checked:
   x  Pearson      or     x Spearman
   x  two-tailed
   x  display actual significance level
  OK
```

For two-way Chi-Square:

```
Statistics
   Summarize
      Crosstabs
         Move Independent Variable to COLUMN (X)
         Move Dependent Variable to ROW (Y)
      Statistics                    Cells
         x  chi square                 x  column
      Continue
   OK
```

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